

# The predictions of cross-power spectrum between 21cm emission and galaxy from the hierarchical galaxy formation model



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- Hierarchical galaxy formation model
- Cross-power spectrum, correlation function
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# Epoch of Reionization (EoR)

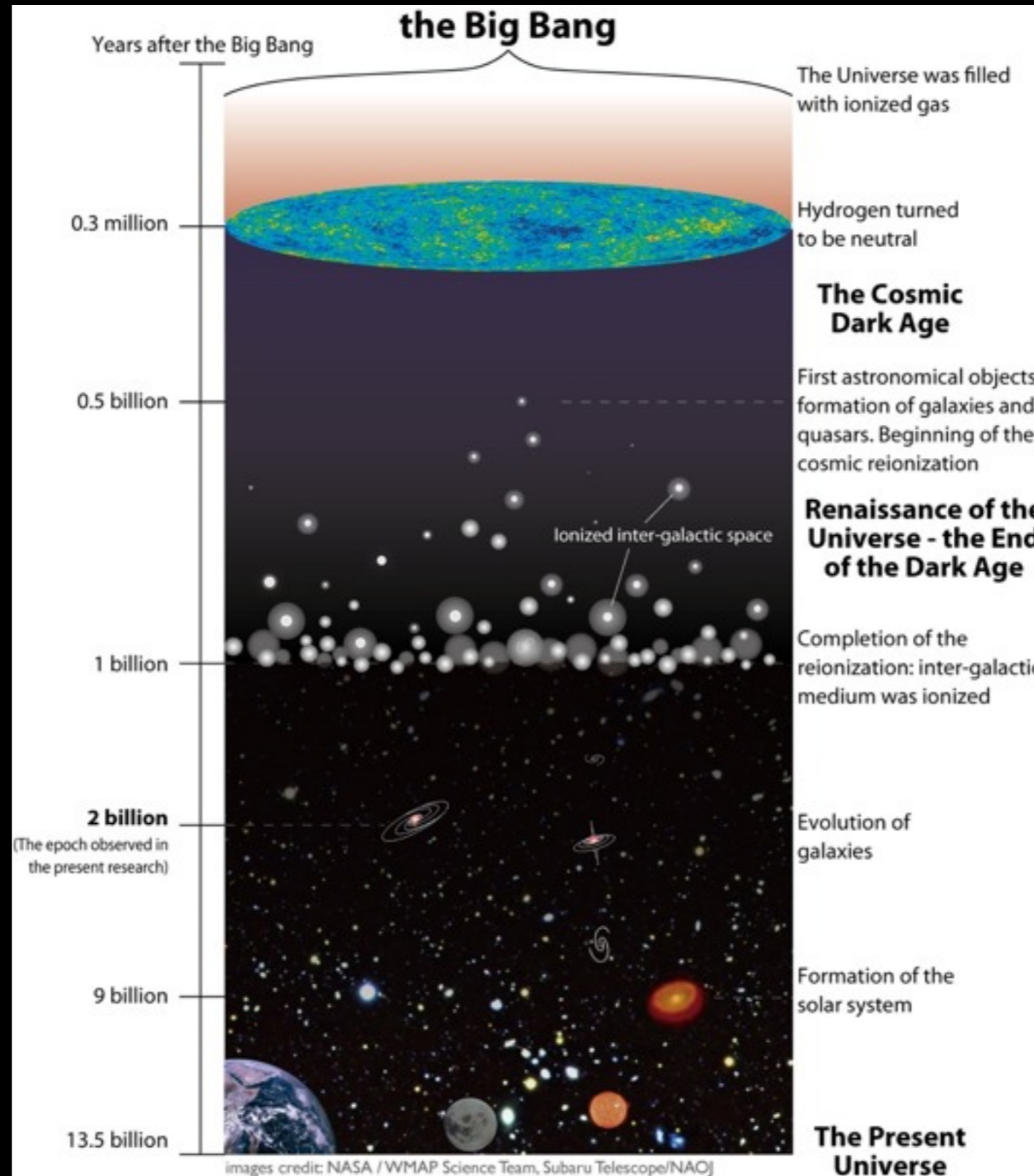


Image Credits: NASA/WMAP

# Epoch of Reionization (EoR)

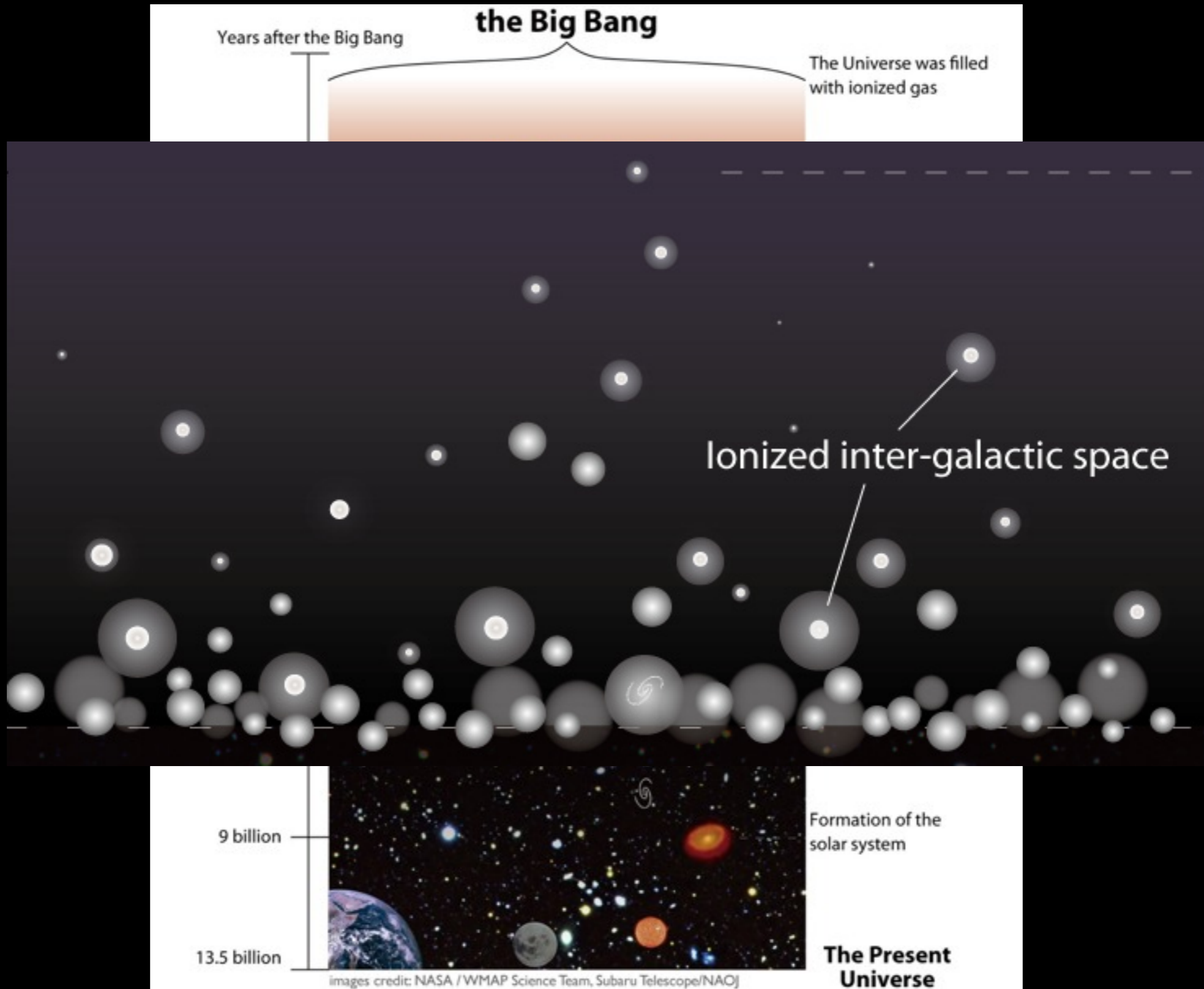


Image Credits: NASA/WMAP

# EoR- Why is the EoR important?

- The EoR is one of the landmark events in the early generations of structure formation.
- identifying when first sources produce high energy photons to ionize neutral IGM
- providing properties of first galaxies and stars

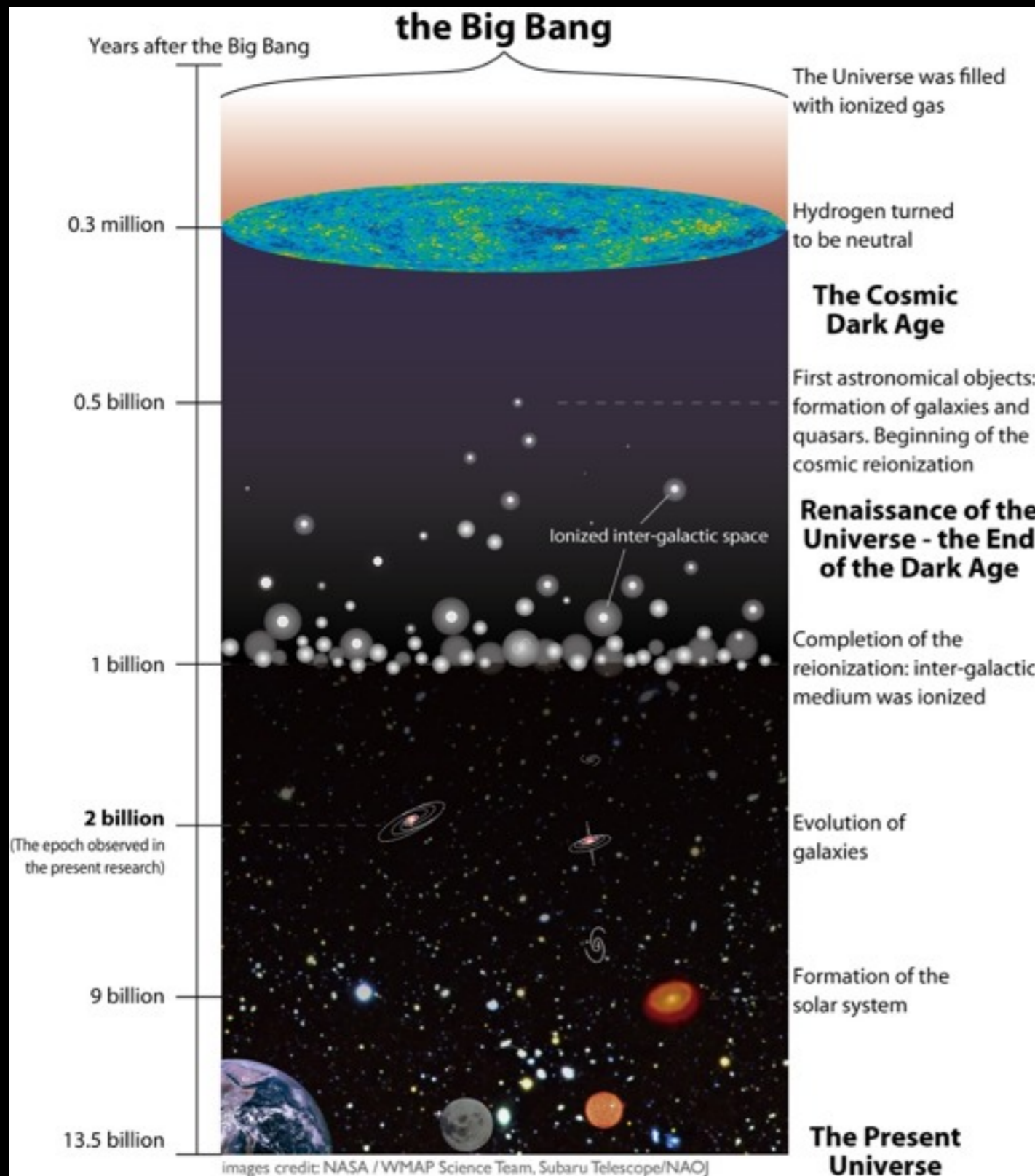


- Early stage of structure formation.

# EoR- Observation

- Thanks to advance of low-frequency instrumentation, several observations are being constructed.
  - Murchison Widefield Array (MWA)
  - The Low Frequency Array (LOFAR)
  - Precision Array to Probe Epoch of Reionization (PAPER)
  - The Square Kilometre Array (SKA)
- They will observe the 21cm signal from HI in IGM.

# The hierarchical galaxy formation model



**GALFORM**  
(Lagos et al. 2012)

AGN feedback

SNe feedback

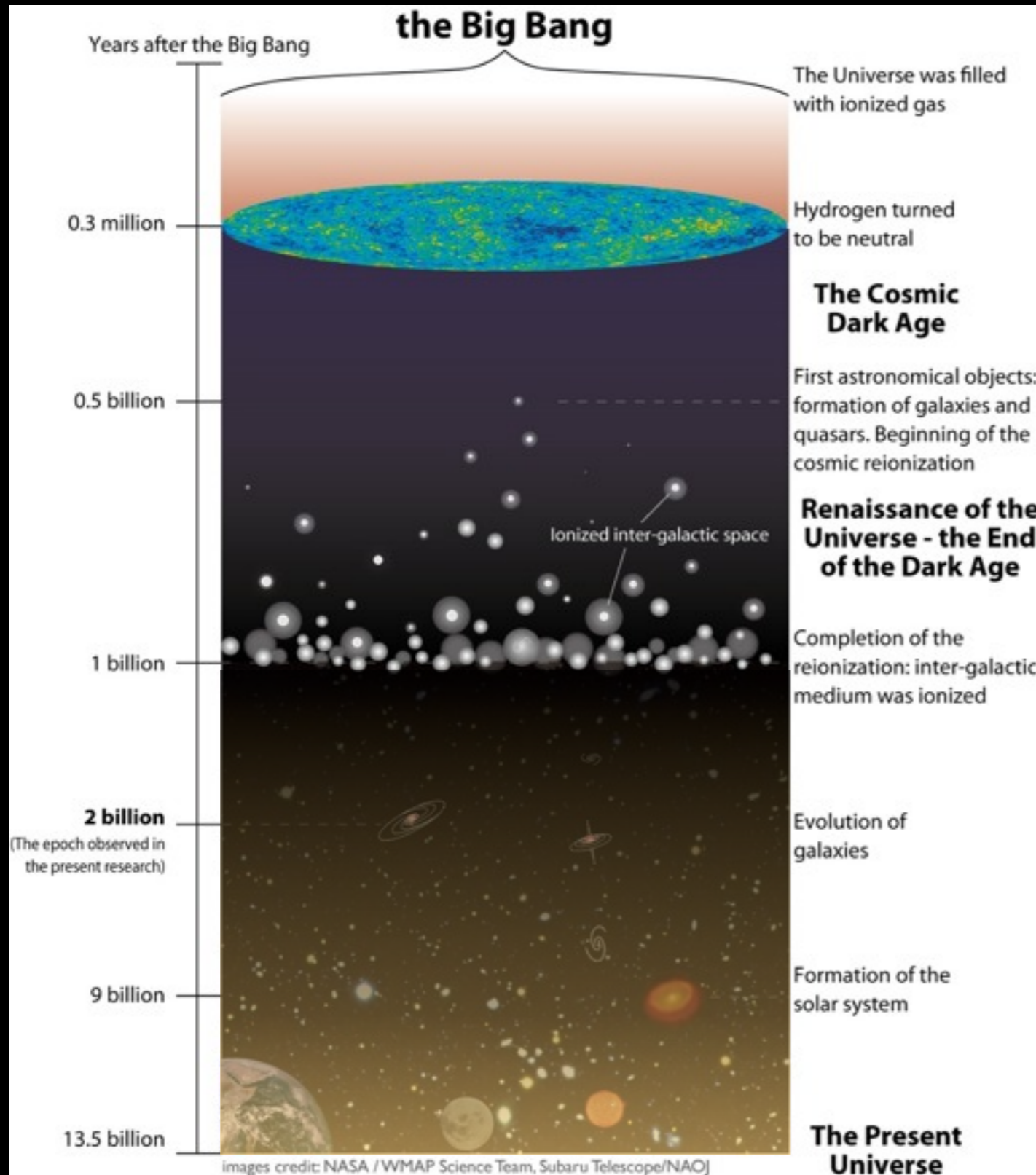
Photoionization feedback



This simulation successfully describes the Universe.

Image Credits: NASA/WMAP

# The hierarchical galaxy formation model



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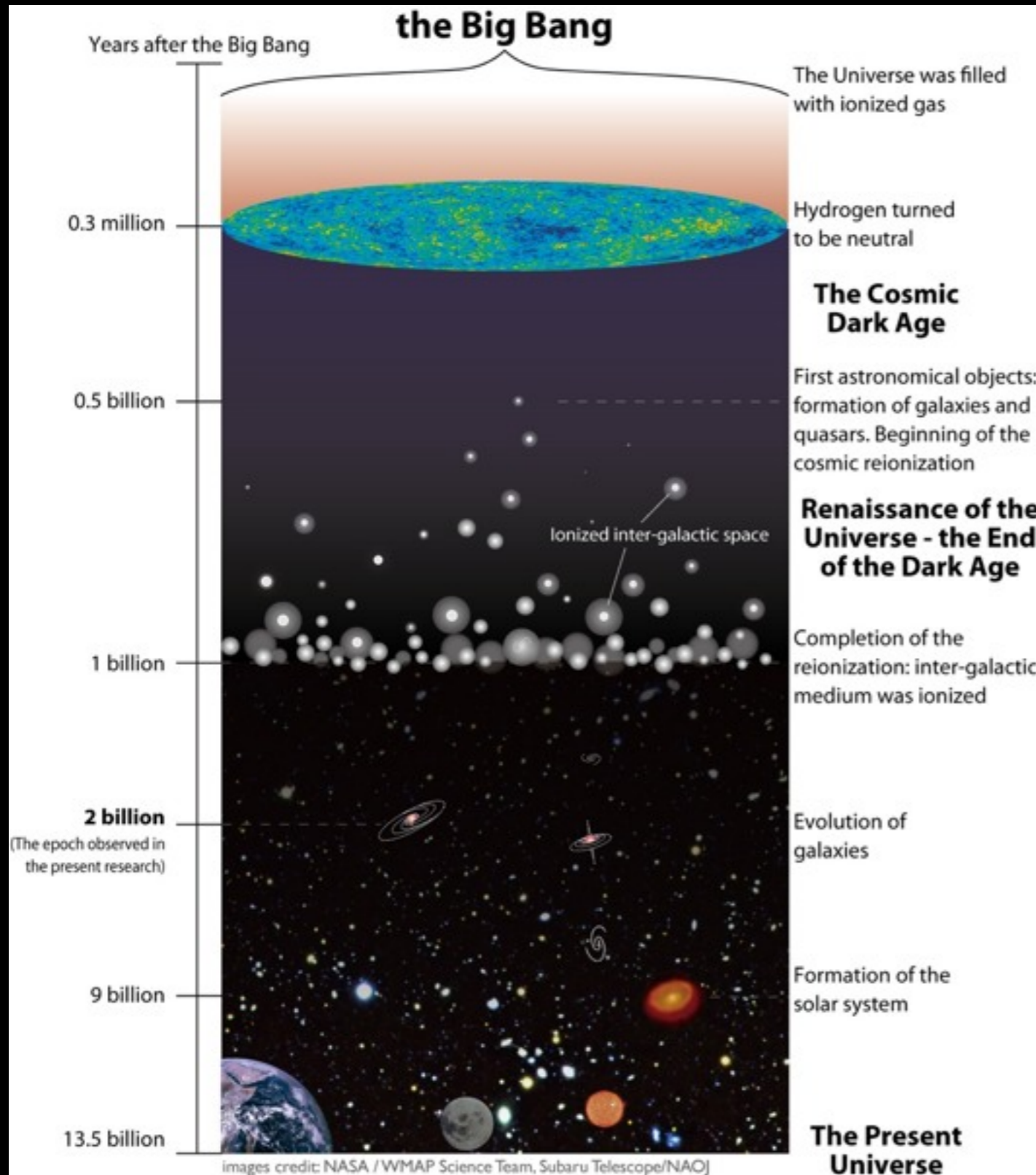


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# The hierarchical galaxy formation model



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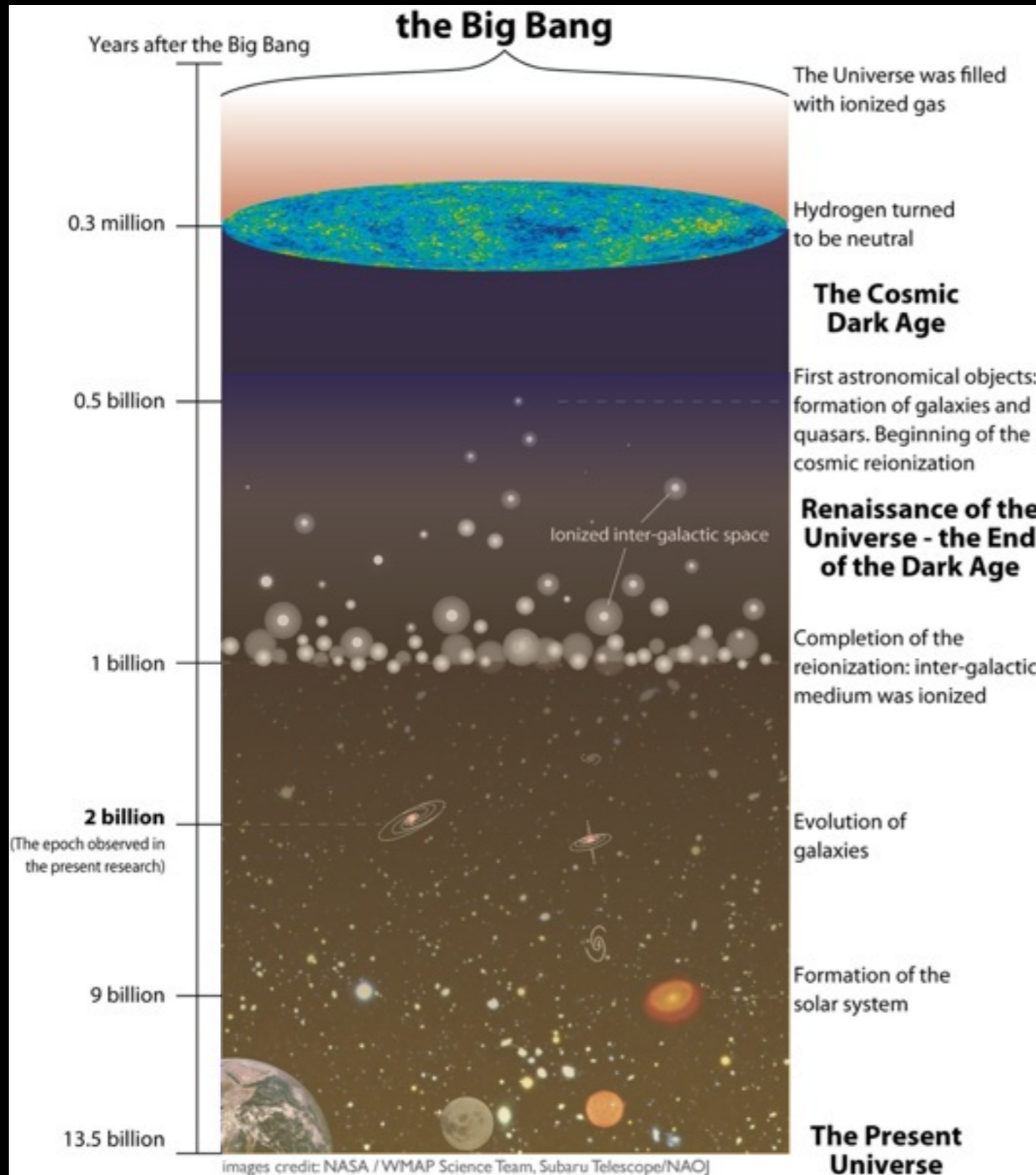
**Semi-Numerical scheme**  
(Kim et al. 2013)



**Self-consistent result**

Image Credits: NASA/WMAP

# The hierarchical galaxy formation model



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**Semi-Numerical scheme**  
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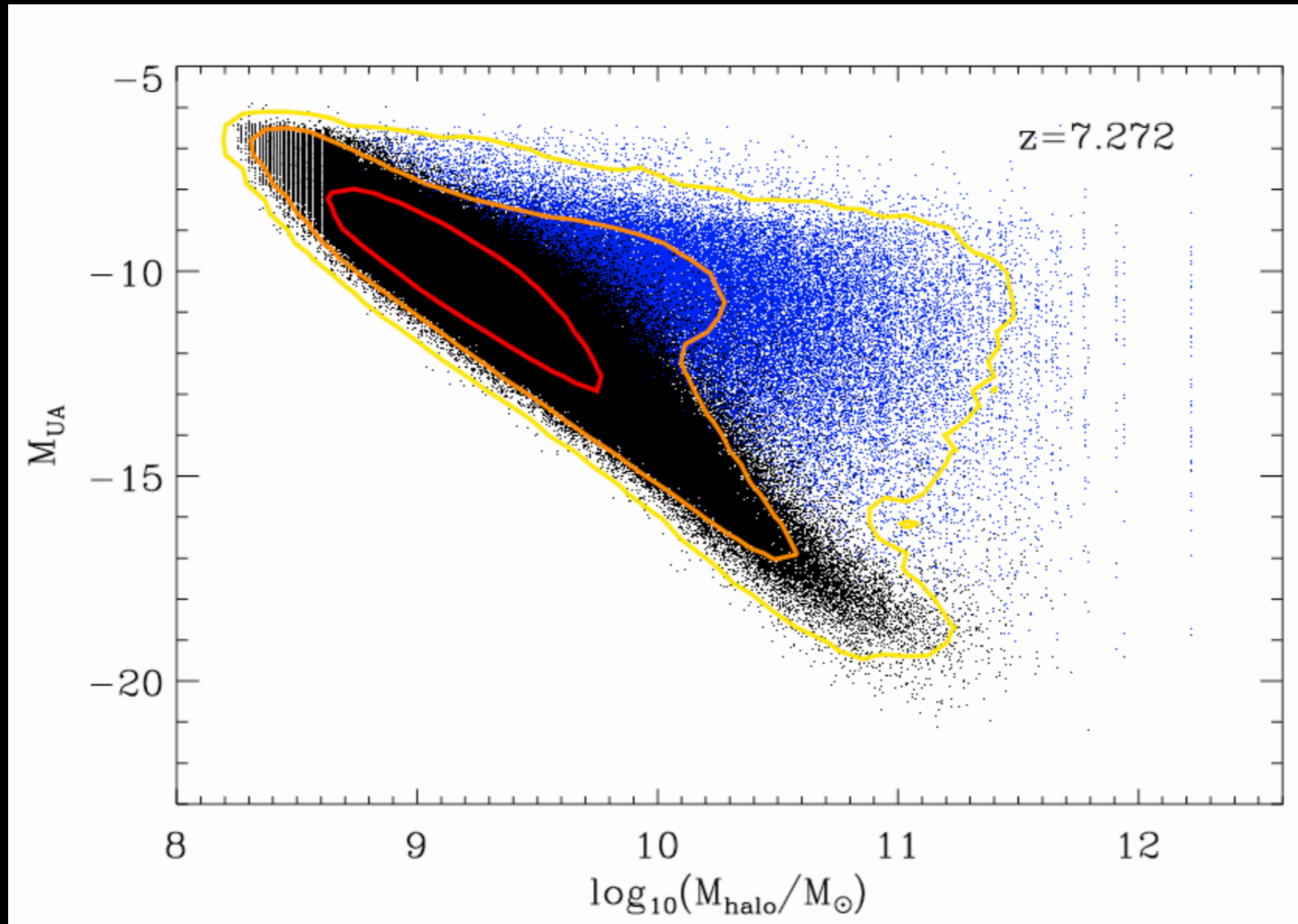


**Self-consistent result**

Image Credits: NASA/WMAP

# The hierarchical galaxy formation model

- Relation between UV magnitude and host halo mass



Luminosity is not simply proportional to dark matter halo mass.

# Powerful method to probe EoR

- The observed cross-power spectrum between 21cm emission and galaxies and its evolution to be sensitive to the astrophysical properties such as...
  - the size of HII regions.
  - clumpiness of the IGM.
  - the nature of the ionizing sources.

# Cross-power spectrum & cross-correlation function

## 21cm brightness temperature

$$\Delta T_{21} = T_0(z)[1 - Q](1 + \delta_{\text{DM,cell}}),$$

$$\text{where } T_0(z) = 23.8 \text{ mK} \left(\frac{1+z}{10}\right)^{\frac{1}{2}}$$

## Cross-power spectrum

$$\langle \hat{\delta}_{21}(\mathbf{k}_1) \hat{\delta}_{\text{gal}}(\mathbf{k}_2) \rangle \equiv (2\pi)^3 \delta_D(\mathbf{k}_1 + \mathbf{k}_2) P_{21,\text{gal}}(\mathbf{k}_1)$$

$$\Delta_{21,\text{gal}}^2(k) = \frac{k^3}{(2\pi^2)} \frac{P_{21,\text{gal}}(k)}{T_0^2(z)}$$

## Cross-correlation function

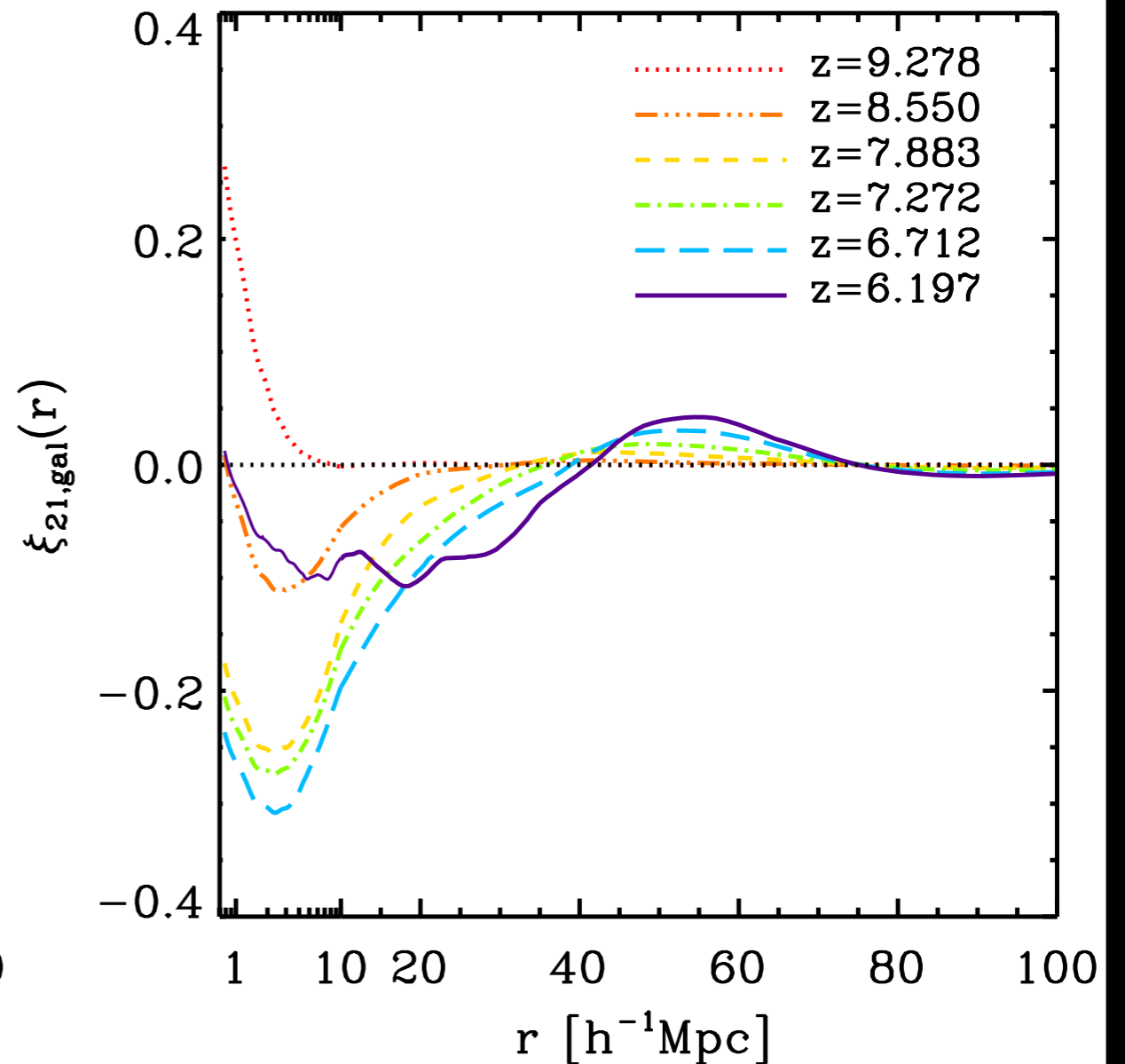
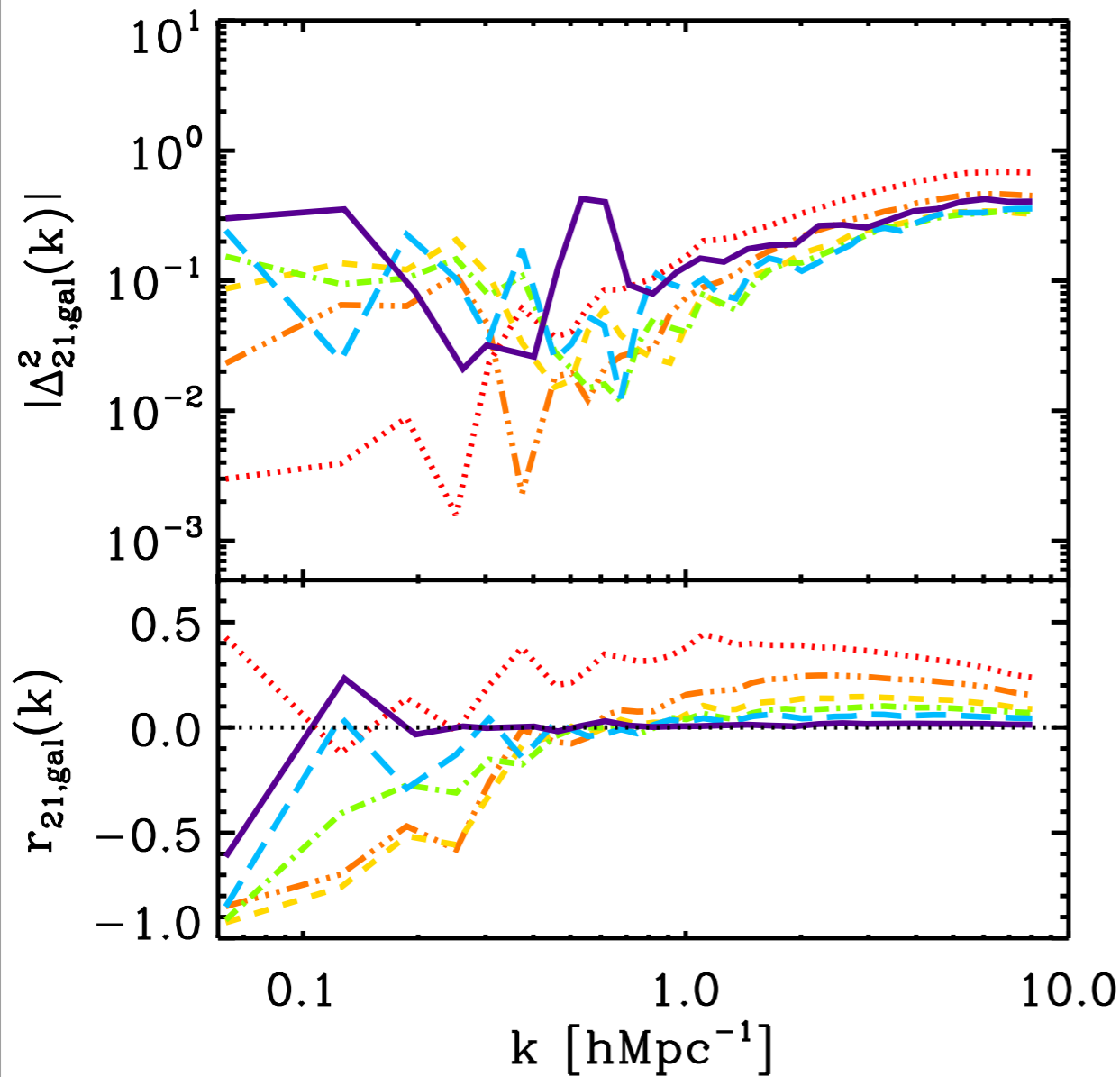
$$\xi_{1,2}(\mathbf{r}) = \langle \delta_1(\mathbf{x}) \delta_2(\mathbf{x} + \mathbf{r}) \rangle$$

## Cross-correlation coefficient

$$r(k) = \frac{P_{21,\text{gal}}(k)}{\sqrt{P_{21}(k)P_{\text{gal}}(k)}} \equiv \frac{A(k)}{\sqrt{B(k)C(k)}}$$

# Cross-power spectrum & cross-correlation function

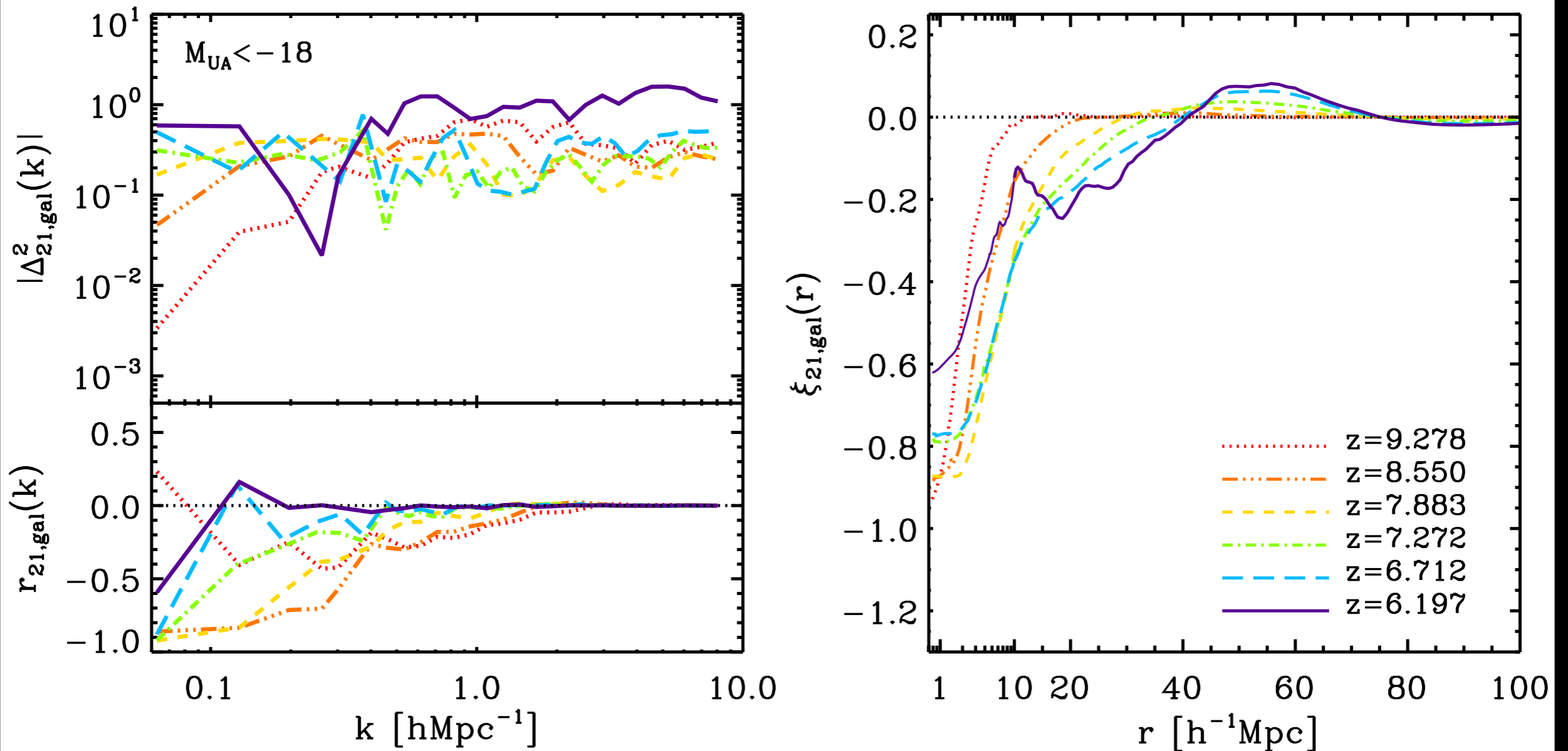
- Redshift evolution of cross-power spectra



The turnover scales imply HII bubble size.

# Cross-power spectrum & cross-correlation function

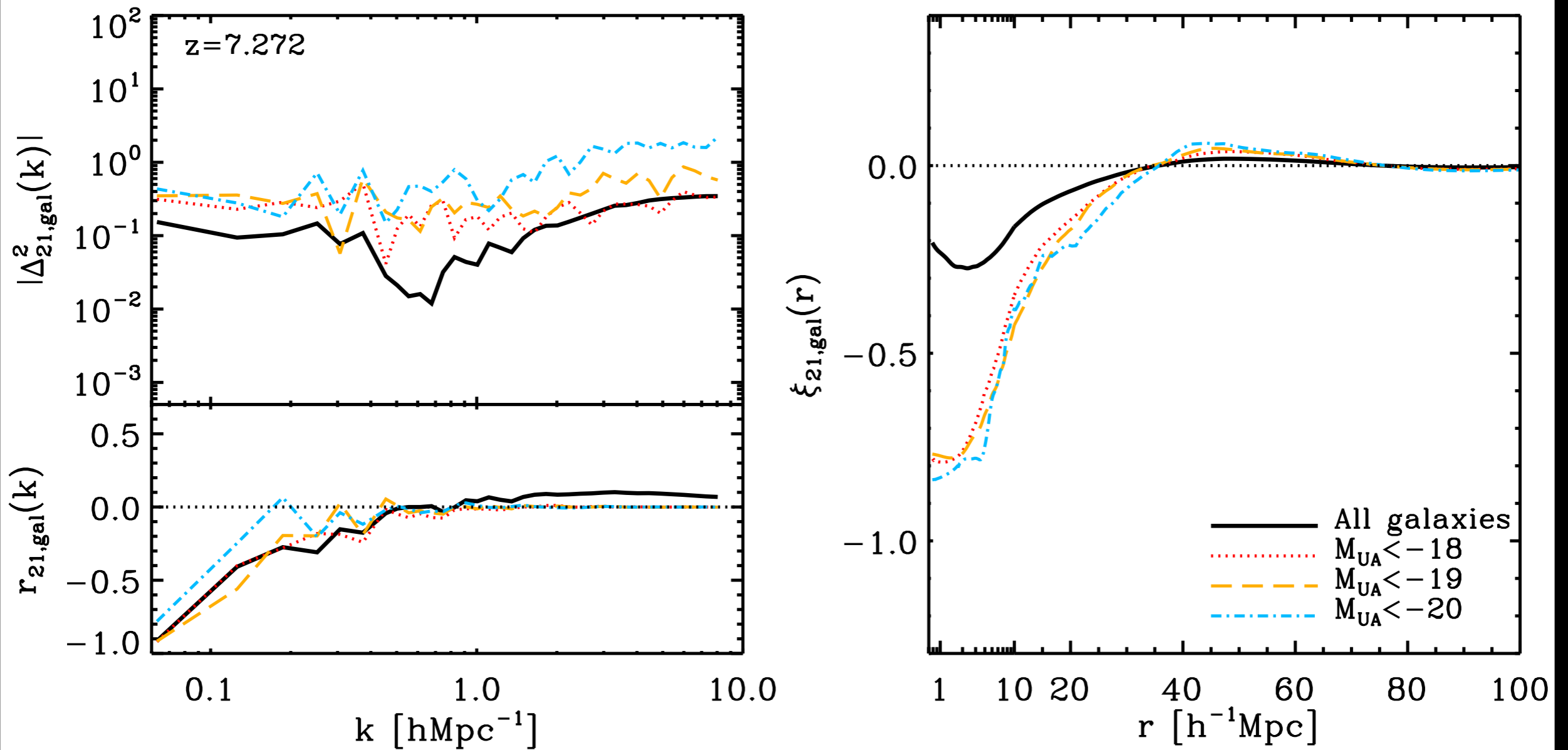
- Redshift evolution of cross-power spectra



Luminous galaxies have strong anti-correlation.

# Cross-power spectrum & cross-correlation function

- Luminosity dependence of cross-power spectra



Bright galaxies have stronger anti-correlation.



# Detectability

We predict detectability of cross-power spectrum using cross-correlation coefficient error based on

- MWA specifications
  - 1000 hours total observing time
  - 800 sqdeg survey area
- Subaru-like galaxy survey & Futuristic galaxy survey
  - galaxy number density:  $1.6 \times 10^{-4} h^3 \text{Mpc}^{-3}$   
 $1.6 \times 10^{-2} h^3 \text{Mpc}^{-3}$
  - redshift error: 0.01

# Detectability

- Predictions of cross-correlation coefficient error

$$\frac{\sigma_r^2}{r^2}(k) = \frac{\sigma_A^2}{A^2}(k) + \frac{\sigma_B^2}{4B^2}(k) + \frac{\sigma_C^2}{4C^2}(k) - \frac{\sigma_{AB}^2}{AB}(k) - \frac{\sigma_{AC}^2}{AC}(k) + \frac{\sigma_{BC}^2}{2BC}(k)$$

$$\begin{aligned} \sigma_A^2(k, \mu) &= \text{var}[P_{21, \text{gal}}(k, \mu)] \\ &= \frac{1}{2} [P_{21, \text{gal}}(k, \mu) + \sigma_B(k, \mu)\sigma_C(k, \mu)] \end{aligned}$$

$$\begin{aligned} \sigma_B^2(k, \mu) &= \text{var}[P_{21}(k, \mu)] \quad \text{Murchison Widefield Array (MWA) specifications} \\ &= \left[ P_{21}(k, \mu) + \frac{T_{\text{sys}}^2}{T_0^2} \frac{1}{Bt_{\text{int}}} \frac{D^2 \Delta D}{n(k_{\perp})} \left( \frac{\lambda^2}{A_e} \right)^2 \right]^2 \end{aligned}$$

system temperature  
 bandpass  
 total observing time  
 antenna array  
 survey volume  
 survey area

$$\begin{aligned} \sigma_C^2(k, \mu) &= \text{var}[P_{\text{gal}}(k, \mu)] \quad \text{Subaru deep survey properties} \\ &= \left[ P_{\text{gal}}(k, \mu) + n_{\text{gal}}^{-1} e^{k_{\parallel}^2 \sigma_x^2} \right]^2 \end{aligned}$$

galaxy number density  
 redshift error

$$\begin{aligned} \sigma_{AB}^2(k, \mu) &= \text{cov}[P_{21, \text{gal}}(k, \mu), P_{21}(k, \mu)] \\ &= [P_{21, \text{gal}}(k, \mu) + P_{21}(k, \mu)] \end{aligned}$$

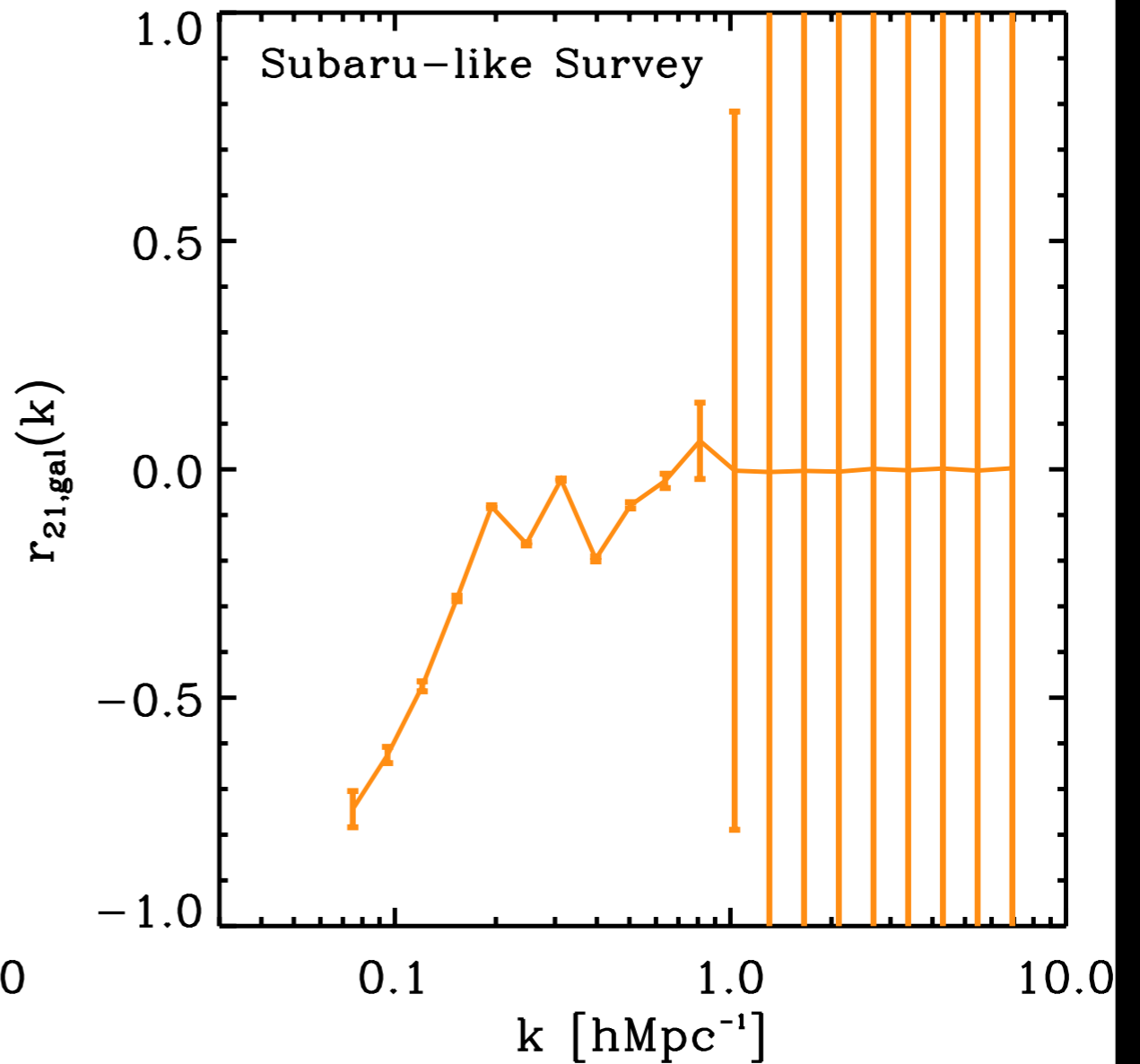
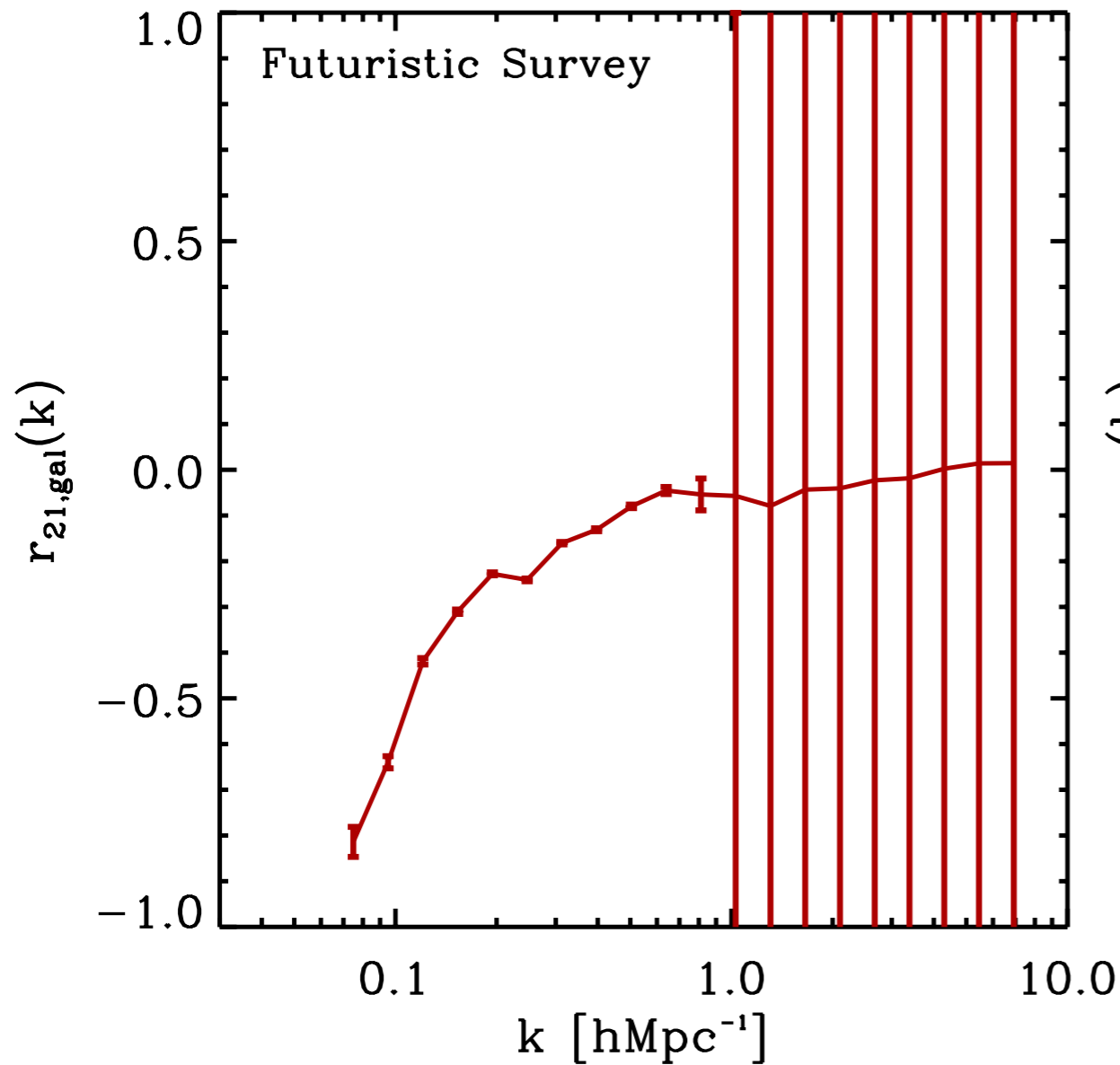
$$\begin{aligned} \sigma_{AC}^2(k, \mu) &= \text{cov}[P_{21, \text{gal}}(k, \mu), P_{\text{gal}}(k, \mu)] \\ &= [P_{21, \text{gal}}(k, \mu) + P_{\text{gal}}(k, \mu)] \end{aligned}$$

$$\begin{aligned} \sigma_{BC}^2(k, \mu) &= \text{cov}[P_{21}(k, \mu), P_{\text{gal}}(k, \mu)] \\ &= [P_{21}(k, \mu) + P_{\text{gal}}(k, \mu)] \end{aligned}$$

Lidz et al., 2009, APJ

# Detectability

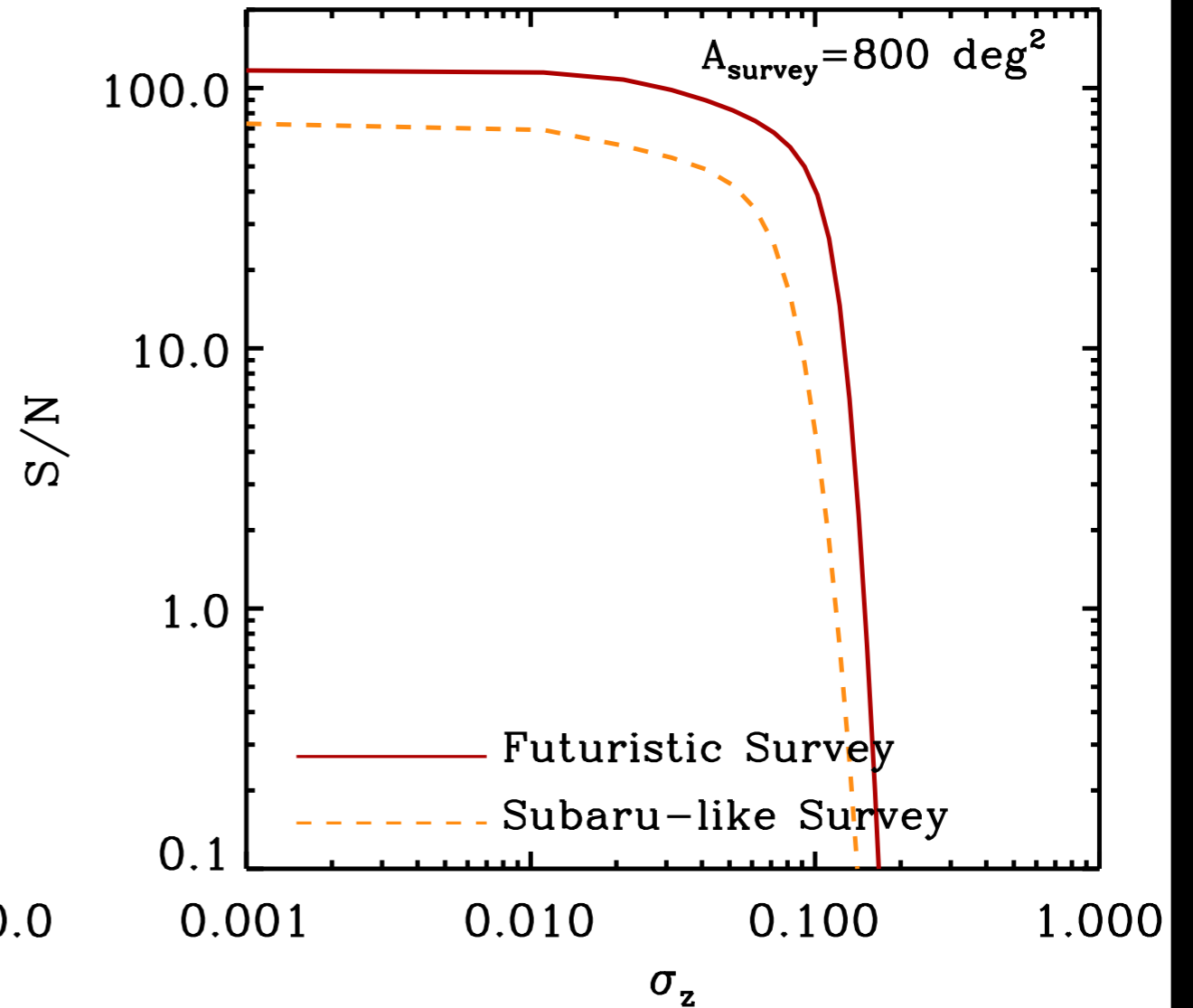
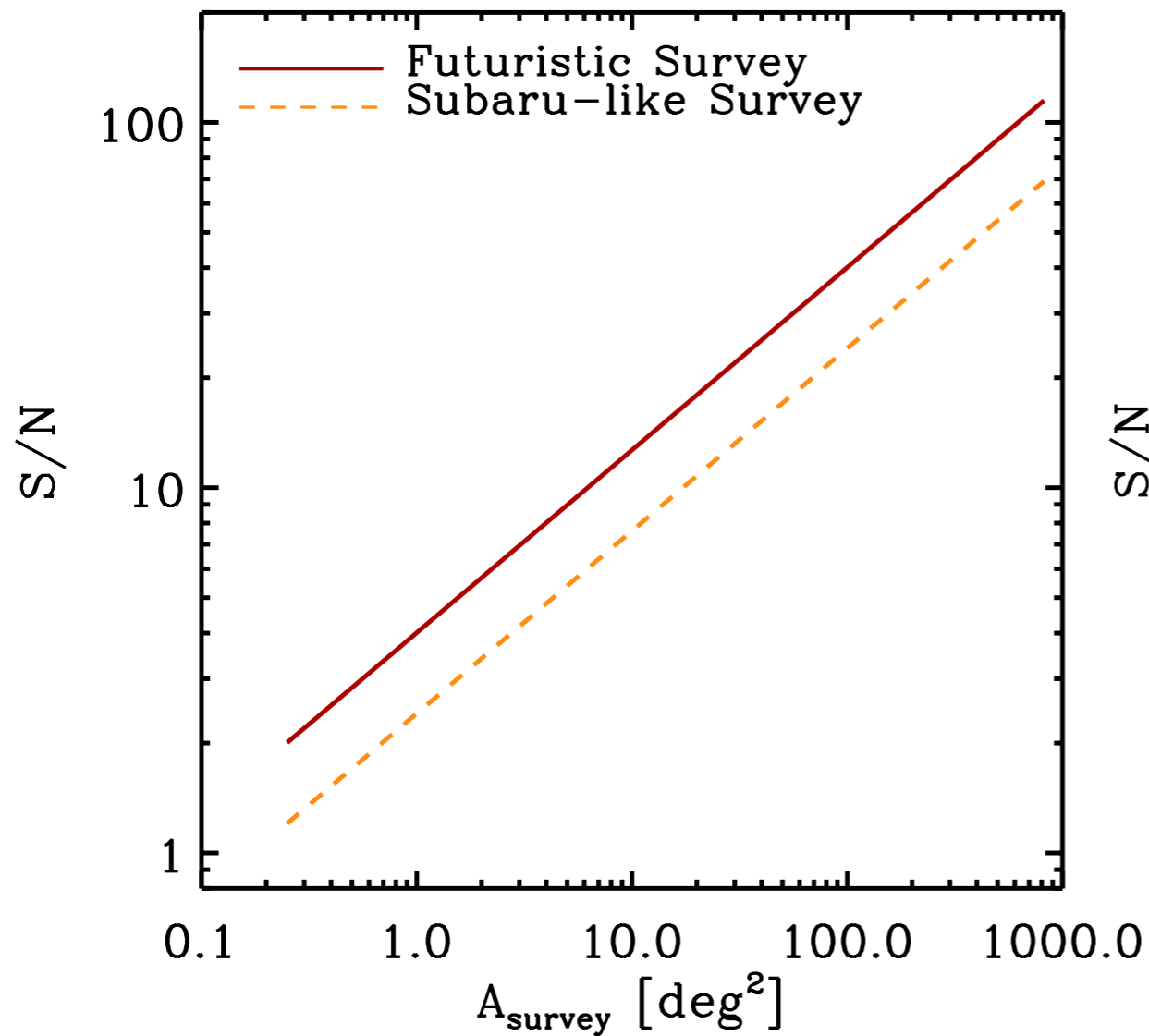
- Predictions of cross-correlation coefficient error



Cross-correlation could be detected at high significance.

# Detectability

## •S/N



Cross-correlation could be detected at high significance.

# Effect of feedback process

- Our model (Lagos et al, 2012)
  - AGN feedback
  - SNe feedback
  - Photoionization feedback
- Modified Bow06 model (Bower et al, 2006)
  - AGN feedback
  - SNe feedback
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# Effect of feedback process

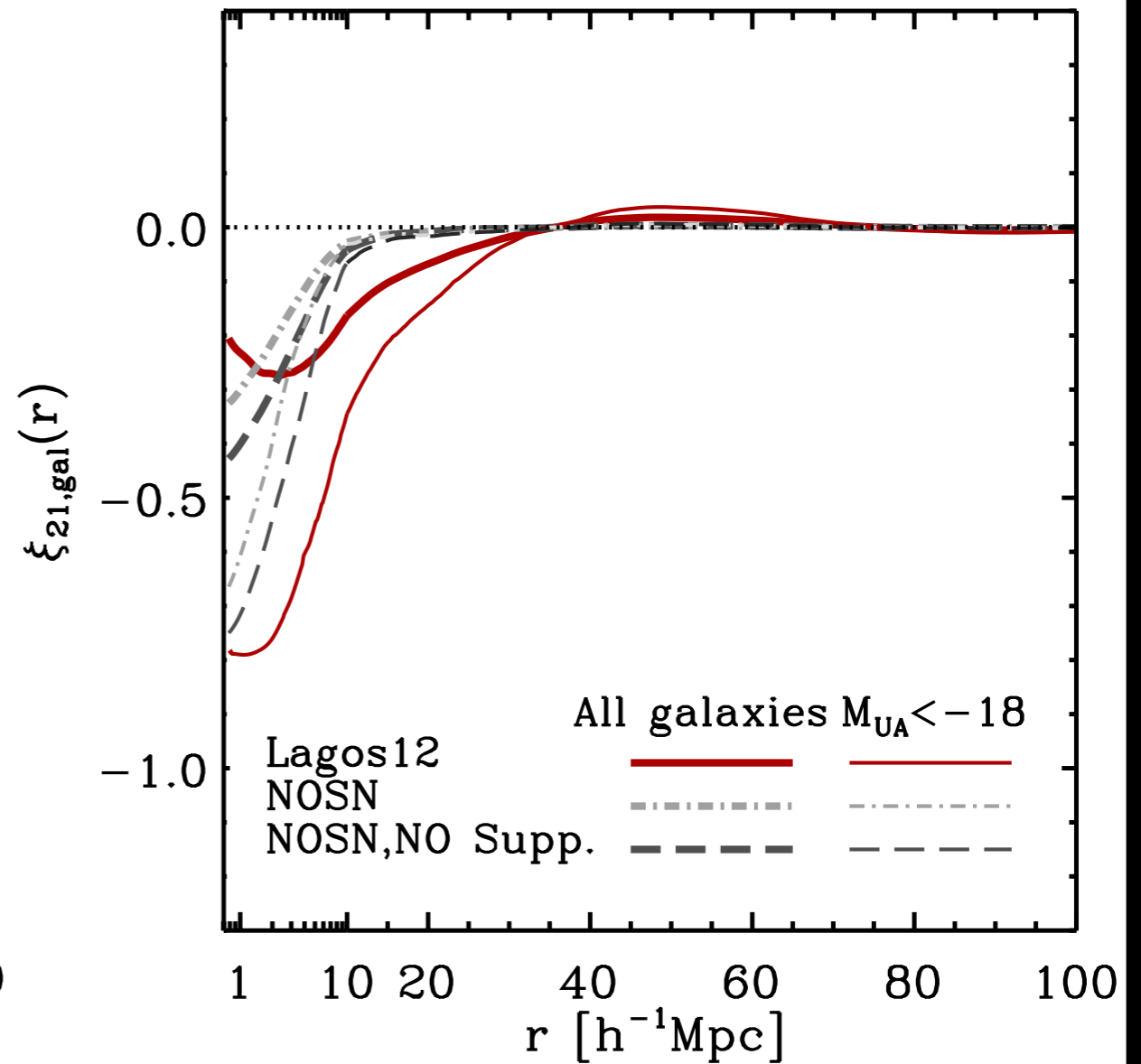
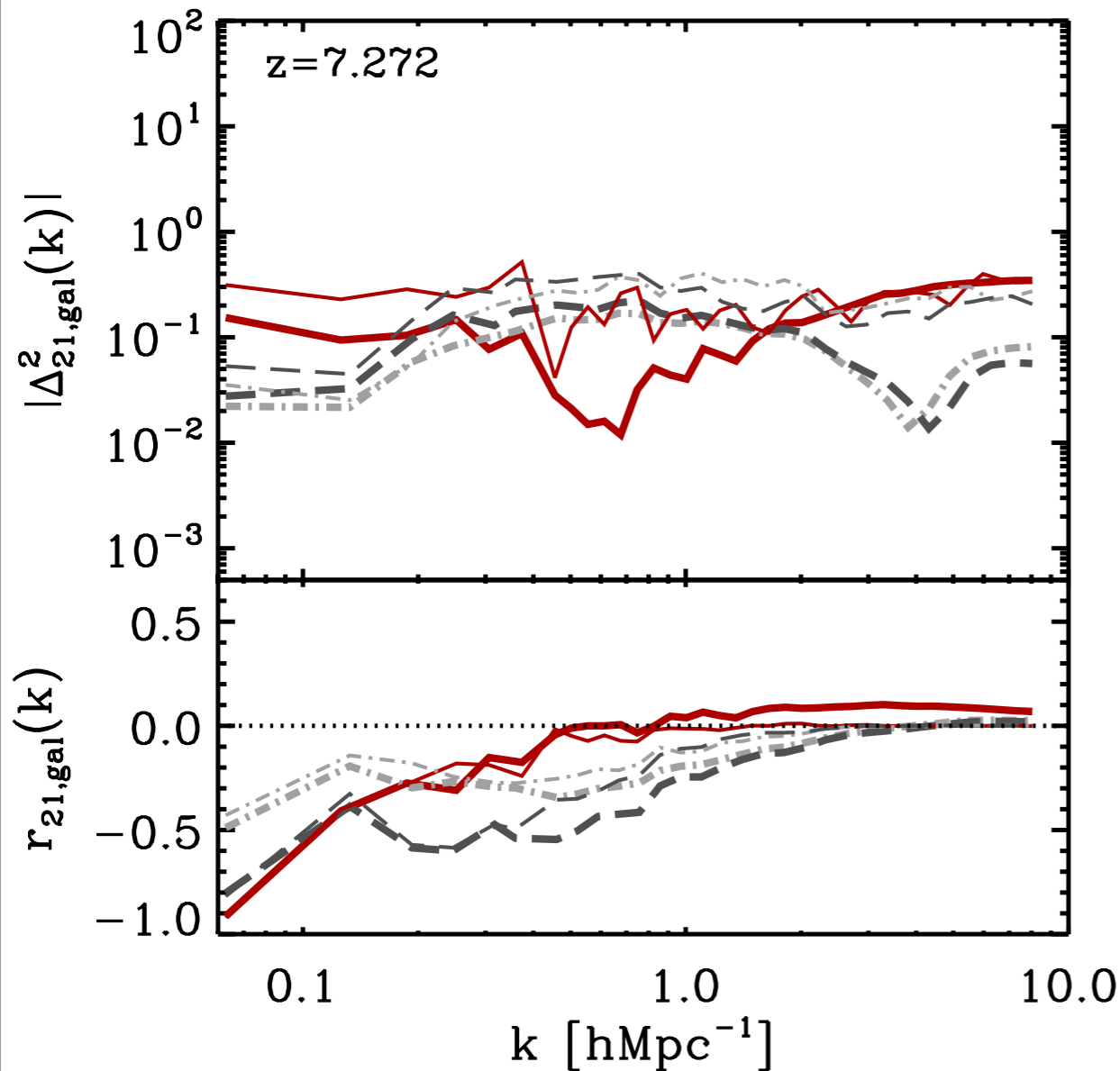
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  - ~~SNe feedback~~ **NOSN**
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# Effect of feedback process

- Our model (Lagos et al, 2012)
  - AGN feedback
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- Modified Bow06 model (Bower et al, 2006)
  - AGN feedback
  - ~~SNe feedback~~ NOSN
  - Photoionization feedback
- Modified Bow06 model (Bower et al, 2006)
  - AGN feedback
  - ~~SNe feedback~~ NOSN
  - ~~Photoionization feedback~~ NO Suppression

# Effect of feedback process

- The effect of feedback process on cross-power spectra

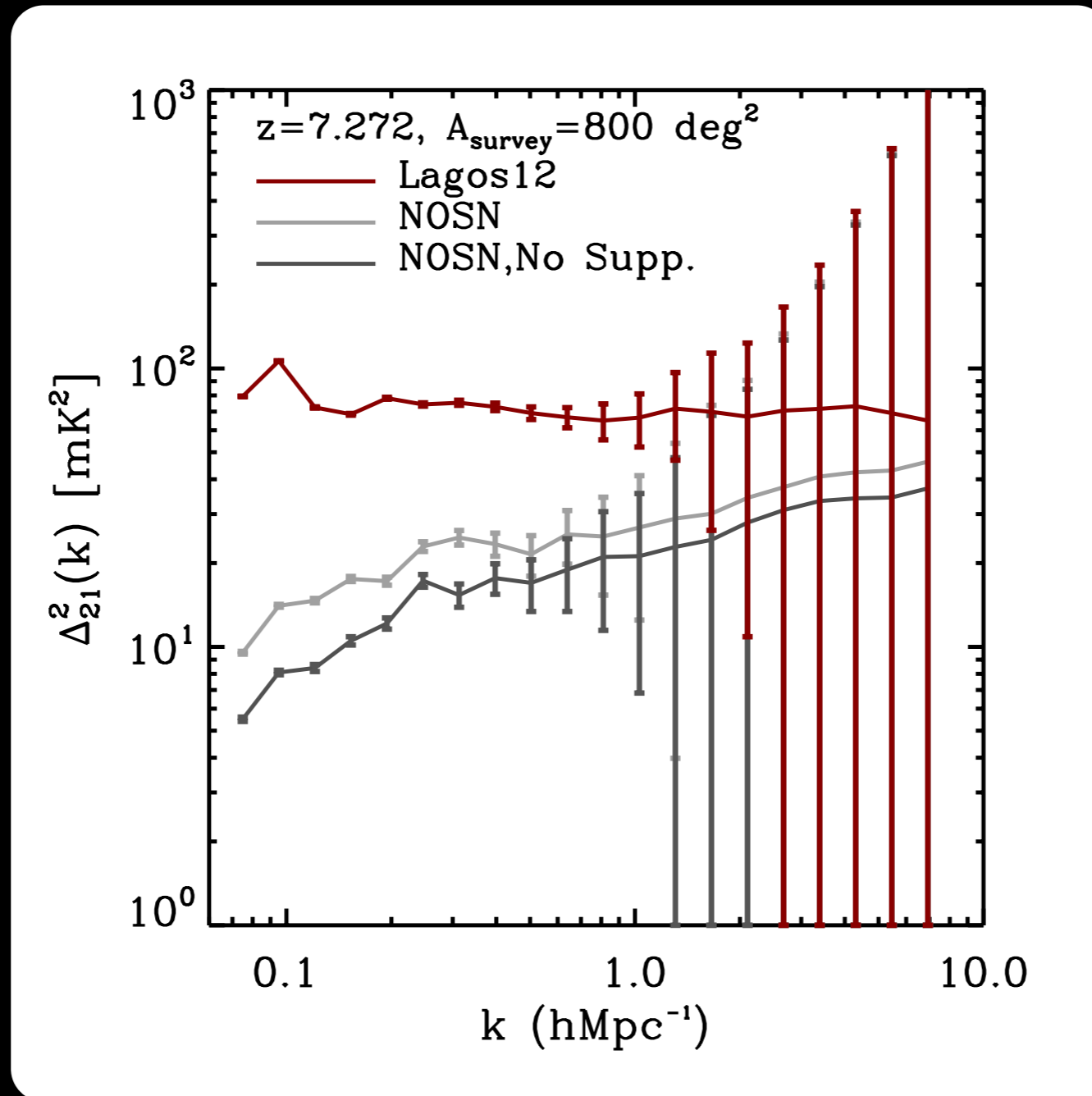


Different feedback processes show different turnover scale.



# Effect of feedback process

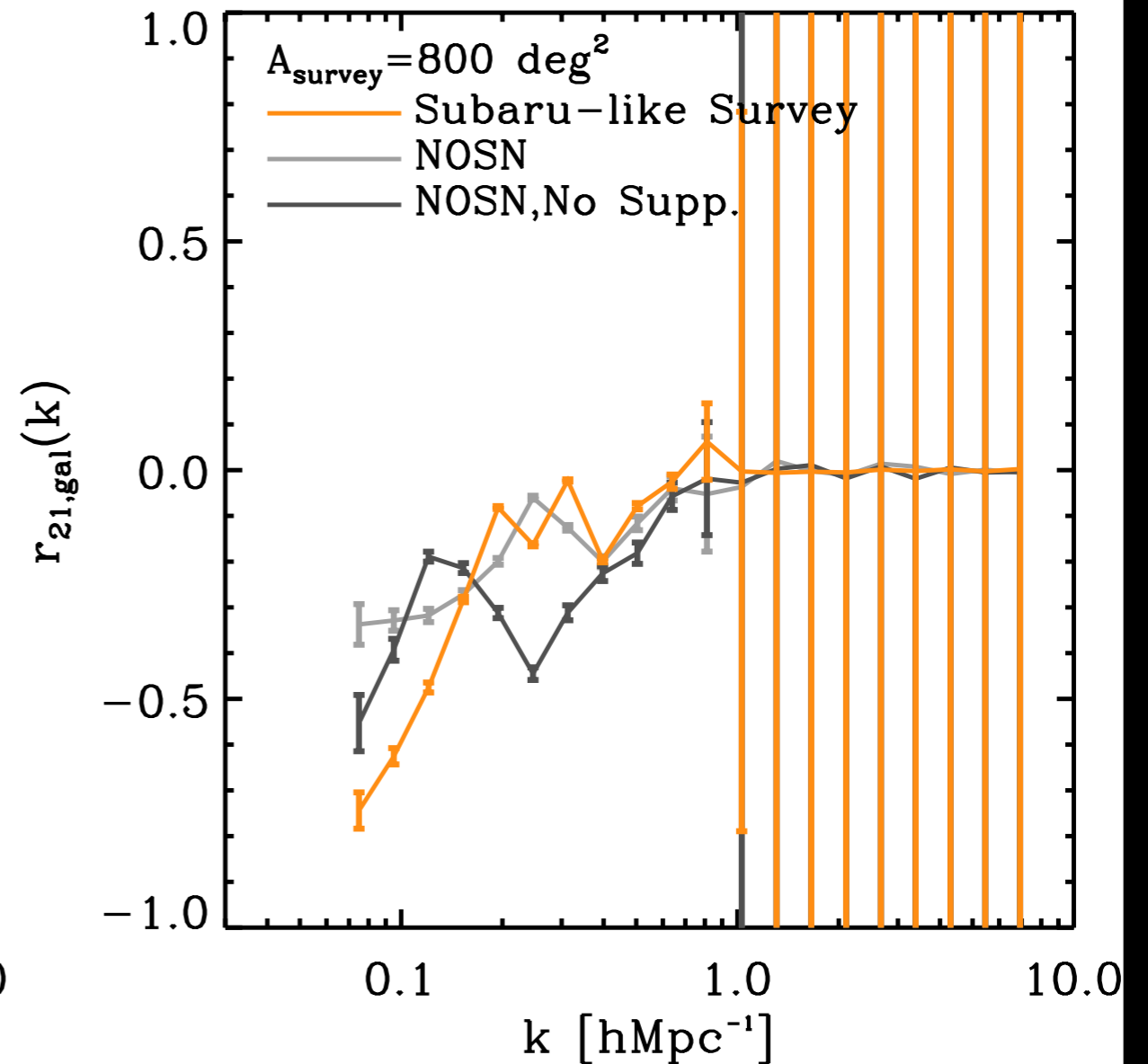
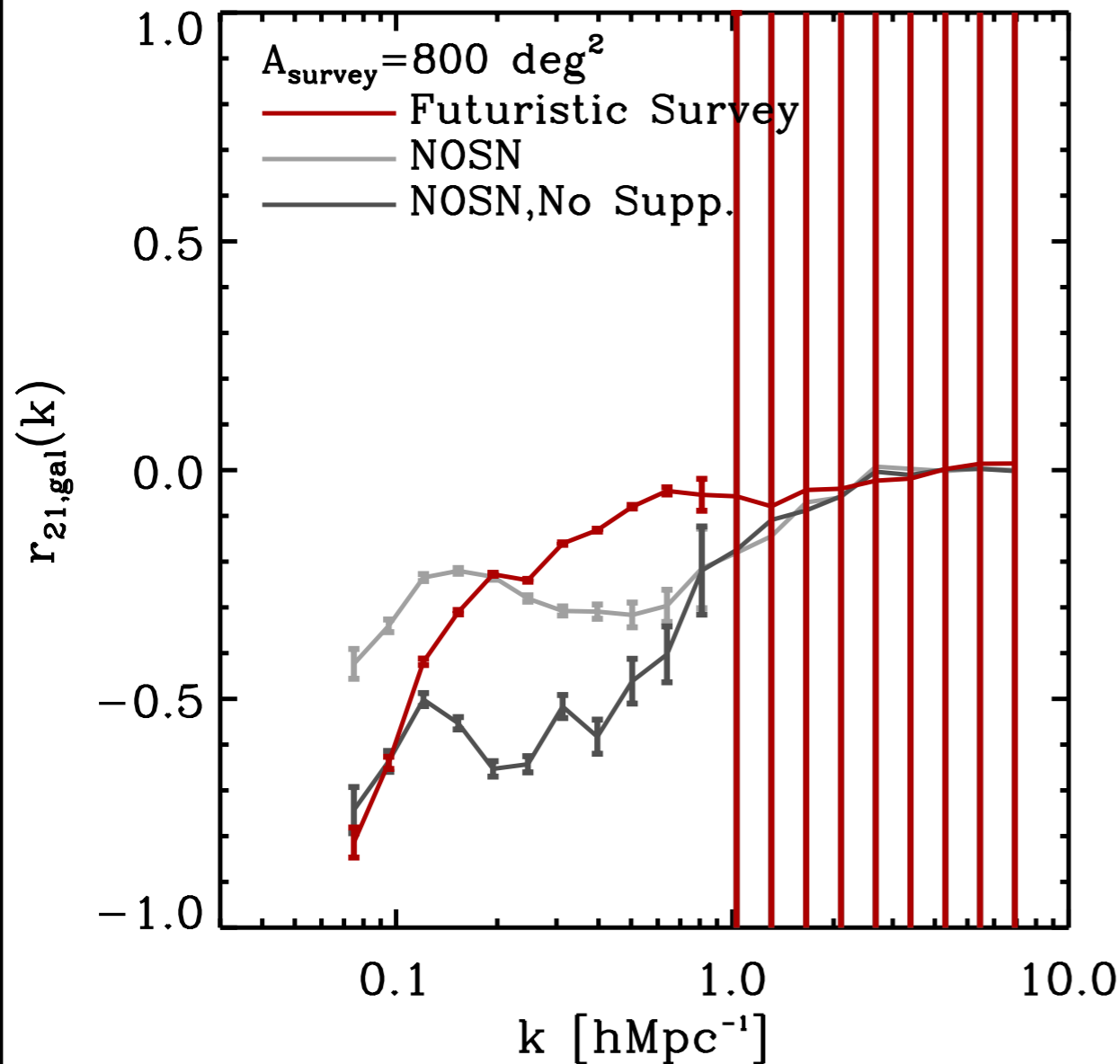
- The effect of feedback process on 21cm power spectra



Different feedback processes affect the shape and error of 21cm power spectra.

# Effect of feedback process

- The effect of feedback process on the detectability



Different feedback processes affect the shape and error of cross-correlation coefficient.

# Summary

- We calculated cross-power spectrum, cross-correlation function, and cross-correlation coefficient using Hierarchical galaxy formation model.
- We calculated observational uncertainties of cross-correlation based on MWA specifications and Subaru-like galaxy survey properties.
- We found that feedback processes make difference on cross-power spectra and estimated error. Thus, detailed modelling is required to predict accurate cross-correlation.

Thank you.