

Clumping factors of HII, HeII and HeIII

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Big simulation box and high spatial resolution

- ◆ Sources – PopIII stars, galaxies, quasars – high σ peaks (100s Mpc box) [e.g. Barkana & Loeb 2004] at high mass resolution [e.g. Bolton & Haehnelt 2007].
- ◆ Resolving IGM (~ 10 kpcs) [e.g. Schaye 2001; McQuinn et al. 2007] and ionized bubbles (\sim Mpc) [e.g. Wyithe & Loeb 2004].

100 cMpc box with
10s kpc spatial resolution

Clumping factors

For example, in the case of a H only simulation, the ionization balance is given by –

$$\frac{d}{dt}n_{\text{HI}} = -3Hn_{\text{HI}} - n_{\text{HI}}\Gamma + R(T)n_en_{\text{HII}}, \quad (5)$$

This can be re-written as –

$$\frac{d}{dt}\tilde{n}_{\text{HI}} = -3H\tilde{n}_{\text{HI}} - C_I\tilde{n}_{\text{HI}}\tilde{\Gamma} + C_R\tilde{R}\tilde{n}_e\tilde{n}_{\text{HII}}, \quad (7)$$

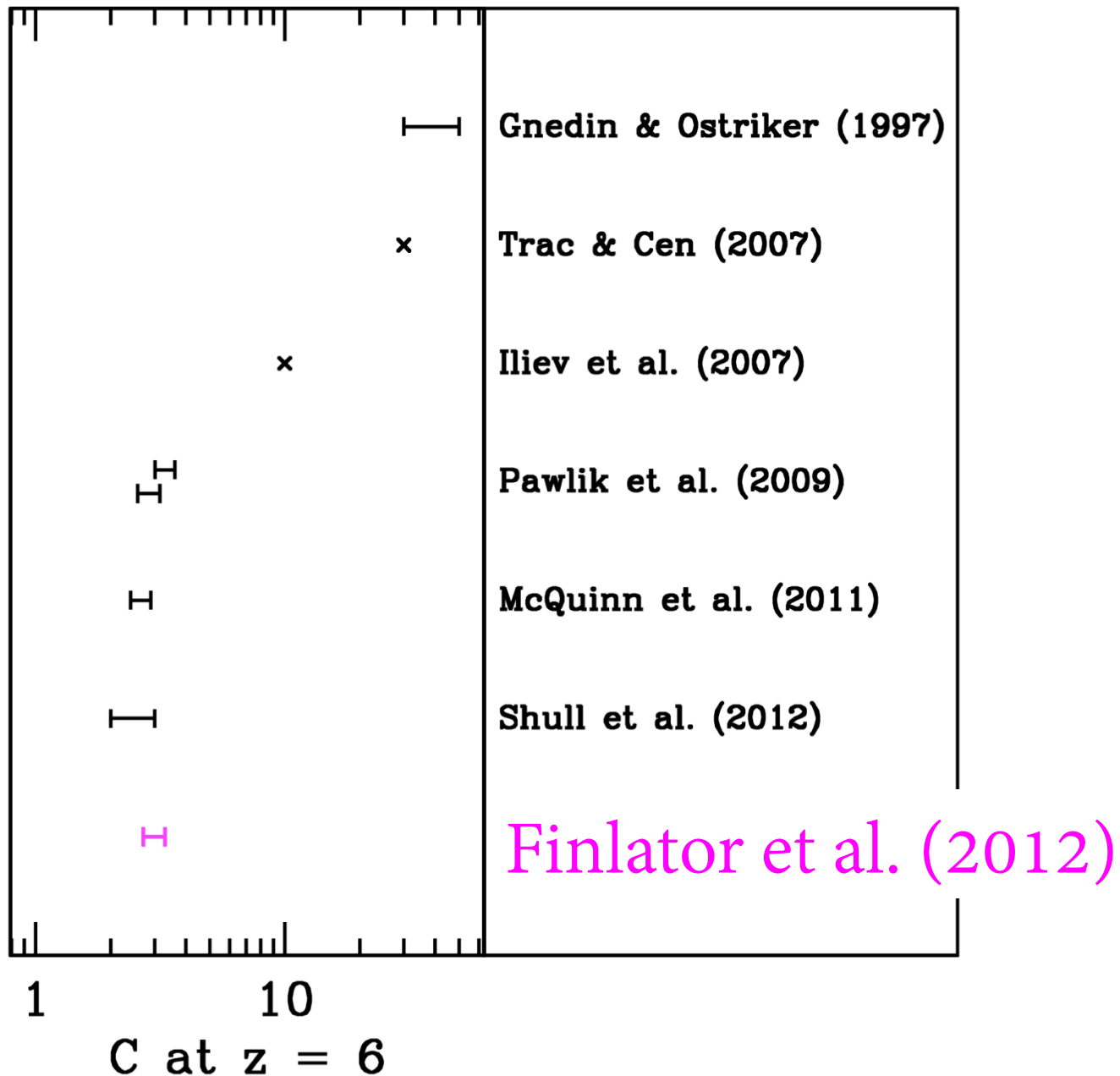
where

$$C_I = \frac{\langle n_{\text{HI}}\Gamma \rangle}{\langle n_{\text{HI}} \rangle \langle \Gamma \rangle},$$

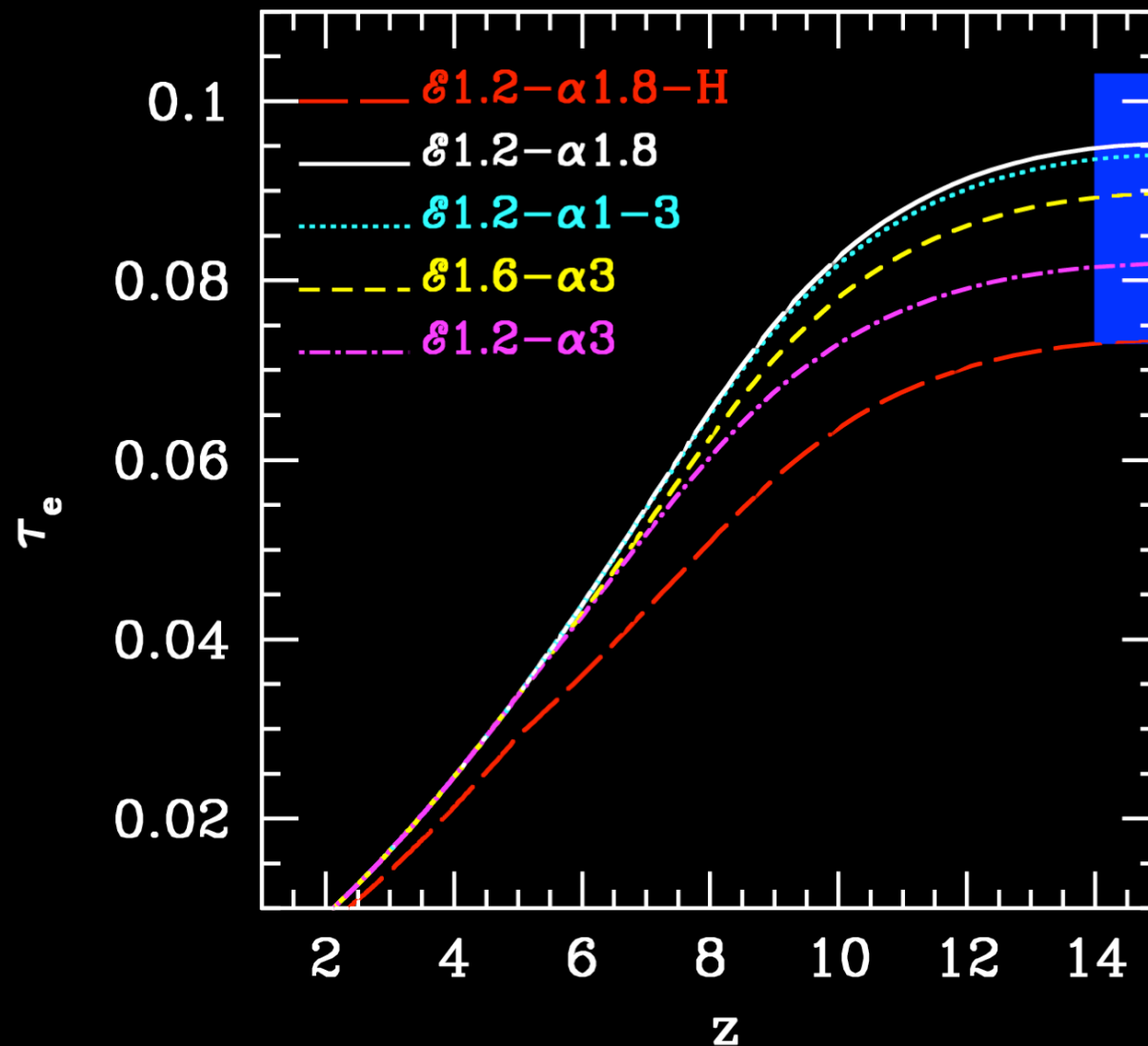
$$C_R = \frac{\langle R(T)n_en_{\text{HII}} \rangle}{\langle R(T) \rangle \langle n_e \rangle \langle n_{\text{HII}} \rangle}.$$

Kohler et al. 2007

IGM clumping factors



Helium is important to get the electron density and temperatures correct



Therefore, we need estimates of H_{ell} and H_{ell} clumping factors along with H_{II} .

Our Simulations

Gadget-3 simulations + CRASH

Box sizes - 2.20, 4.40, 8.80 cMpc/h

Gadget particle number - 2×256^3

CRASH grid size – 32^3 , 64^3 , 128^3 RT cells.

Best RT resolution – 17 ckpc/h

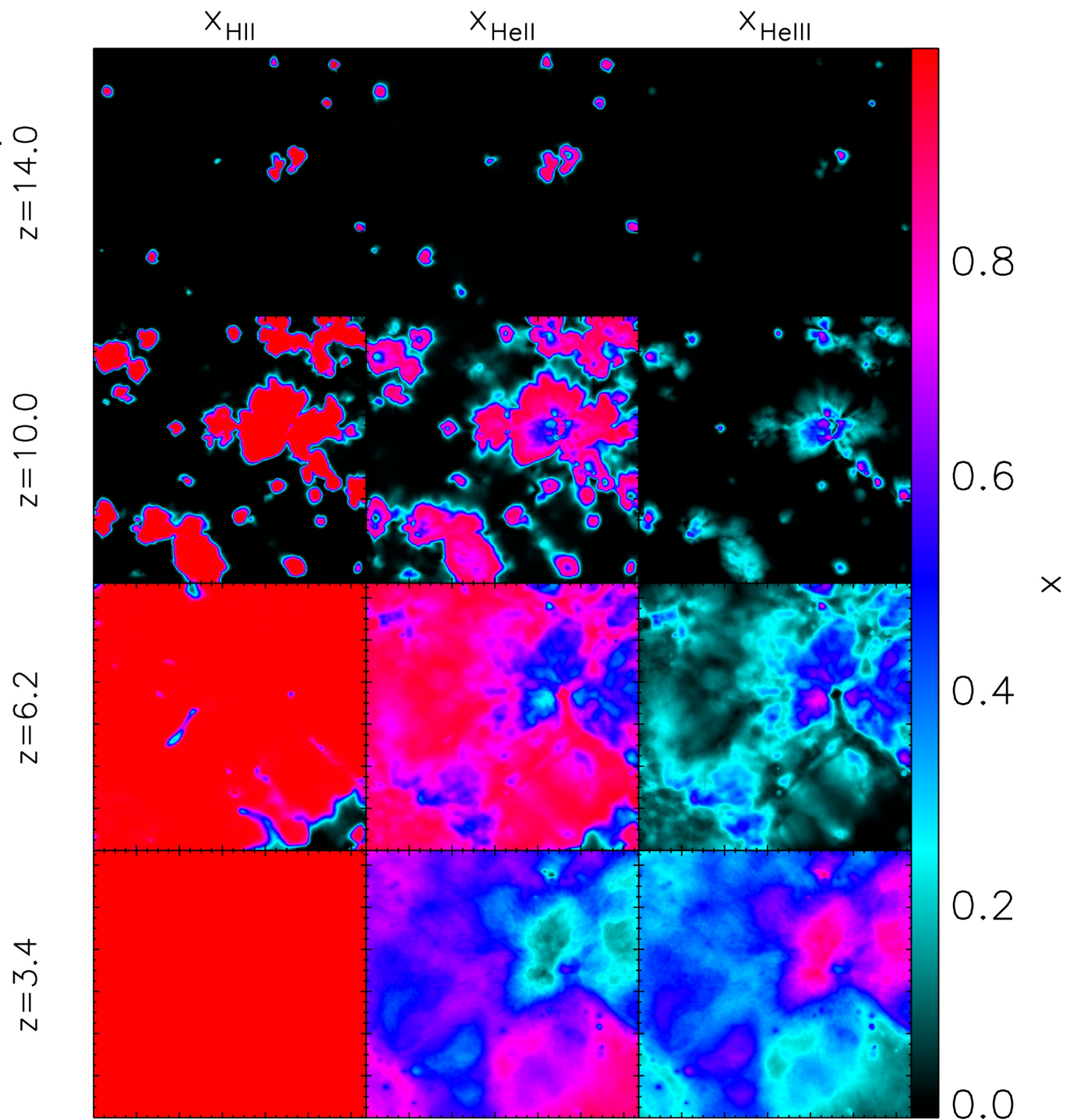
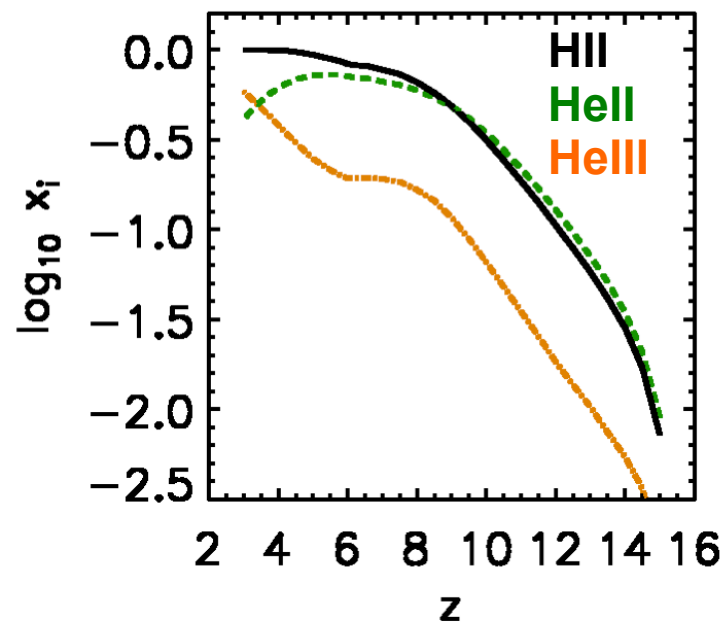
EUV spectral index - $\alpha = 1.8$

No escape fractions assumed – Emissivity calibrated to ‘ τ ’ from WMAP7 (Komatsu et. al 2011) and photo ionization rates computed from observations of Ly α forest at $z \sim 6$ (Bolton et. al 2007).

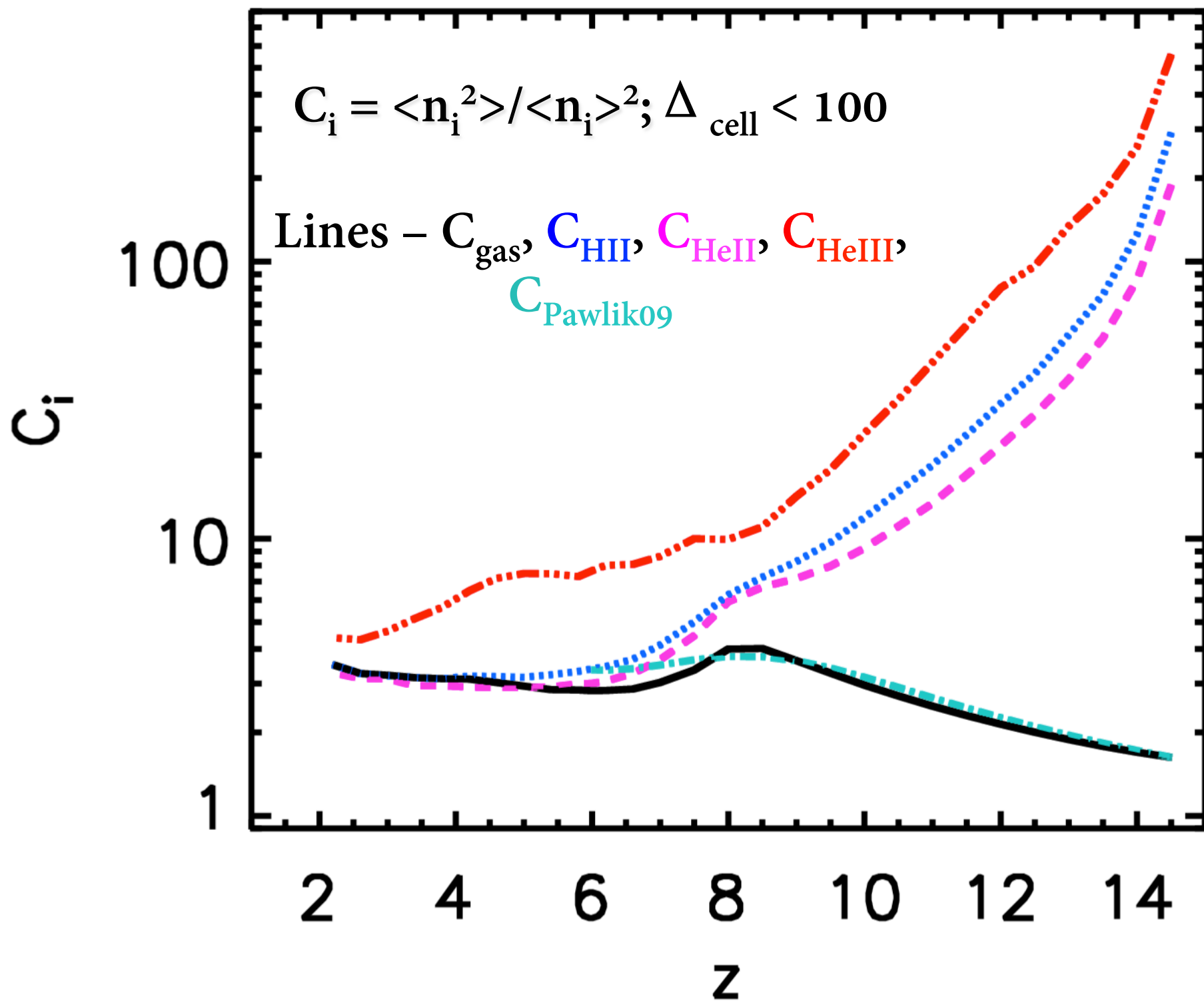
Ciardi, Bolton, Maselli & Graziani 2011

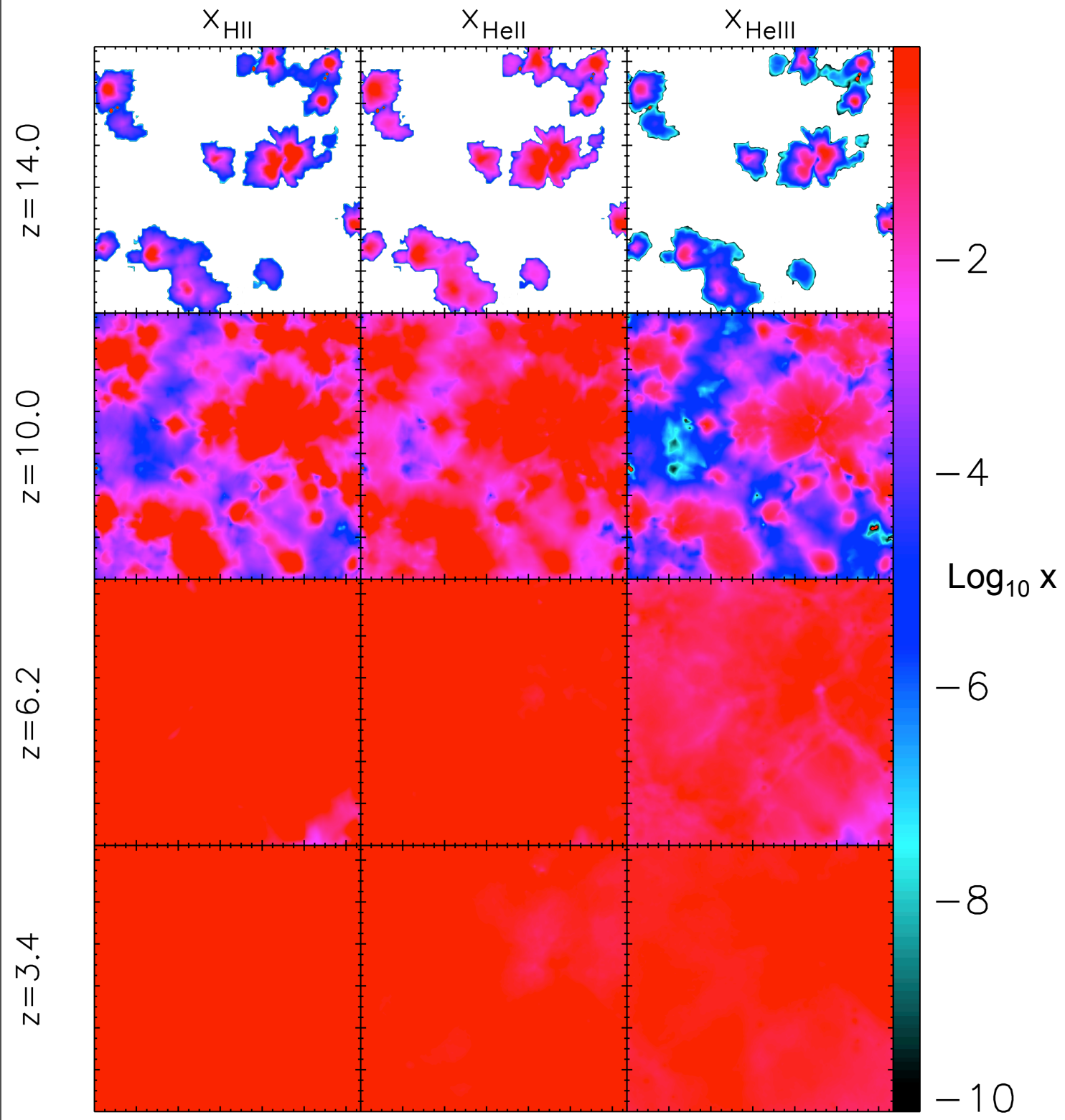
EoR simulation

2.2 cMpc/h
128³ RT



Clumping factor

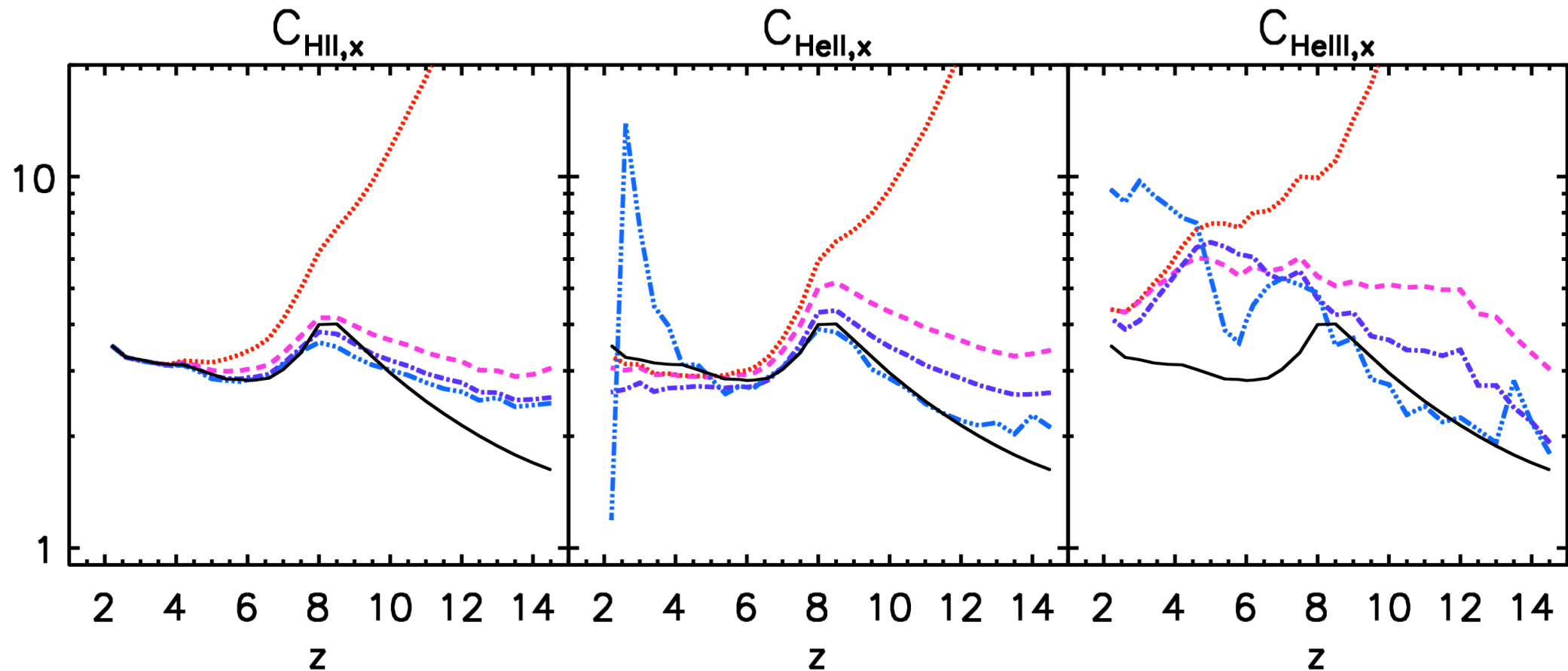




For different ionization thresholds

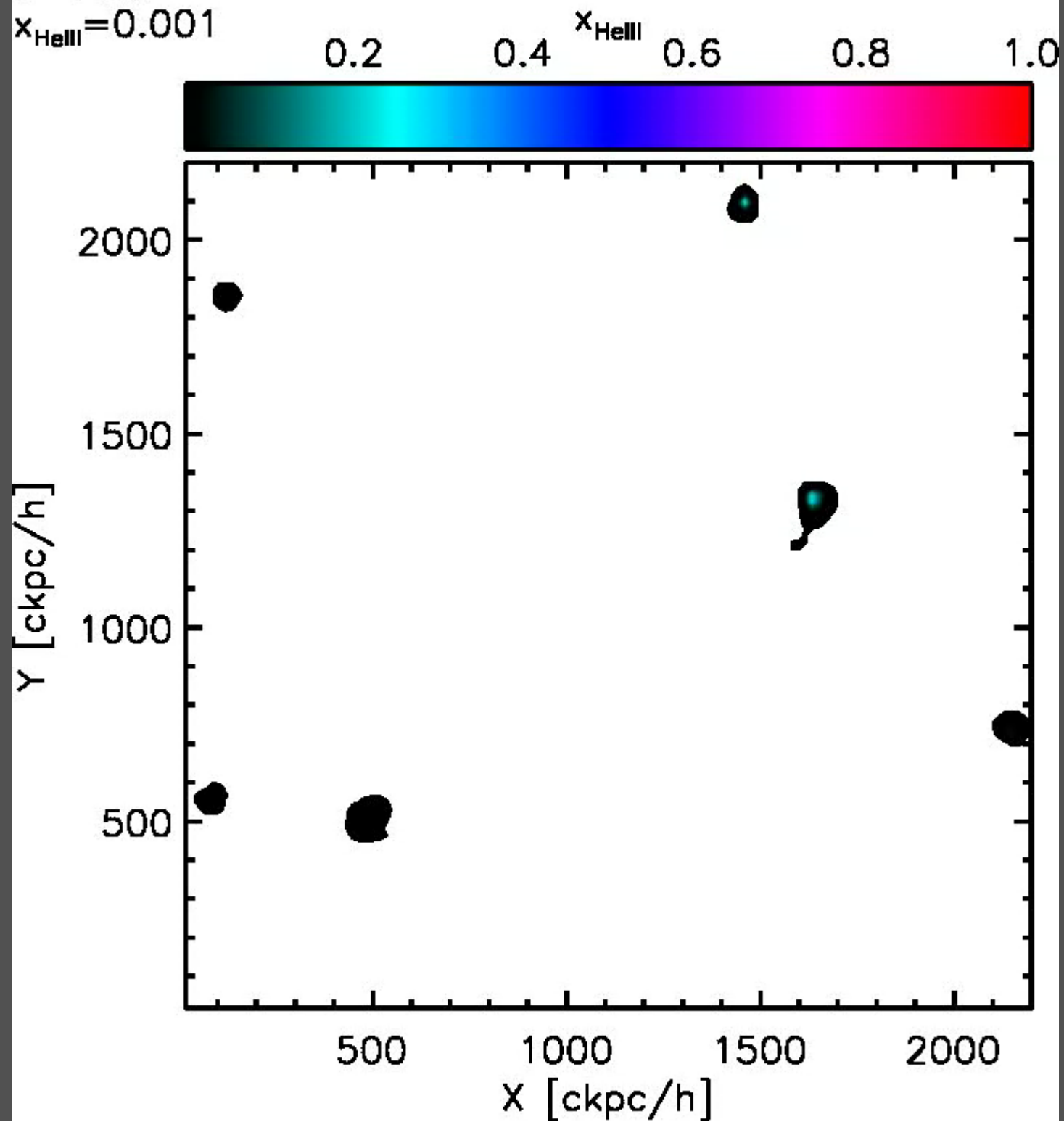
$$C_{i,x} = \langle n_i^2 \rangle_{(x > x_{th})} / \langle n_i \rangle_{(x > x_{th})}^2$$

$\Delta_{\text{cell}} < 100$; Lines – C_{gas} , $x > 0$, $x > 0.1$, $x > 0.5$, $x > 0.9$



$z=14.8$

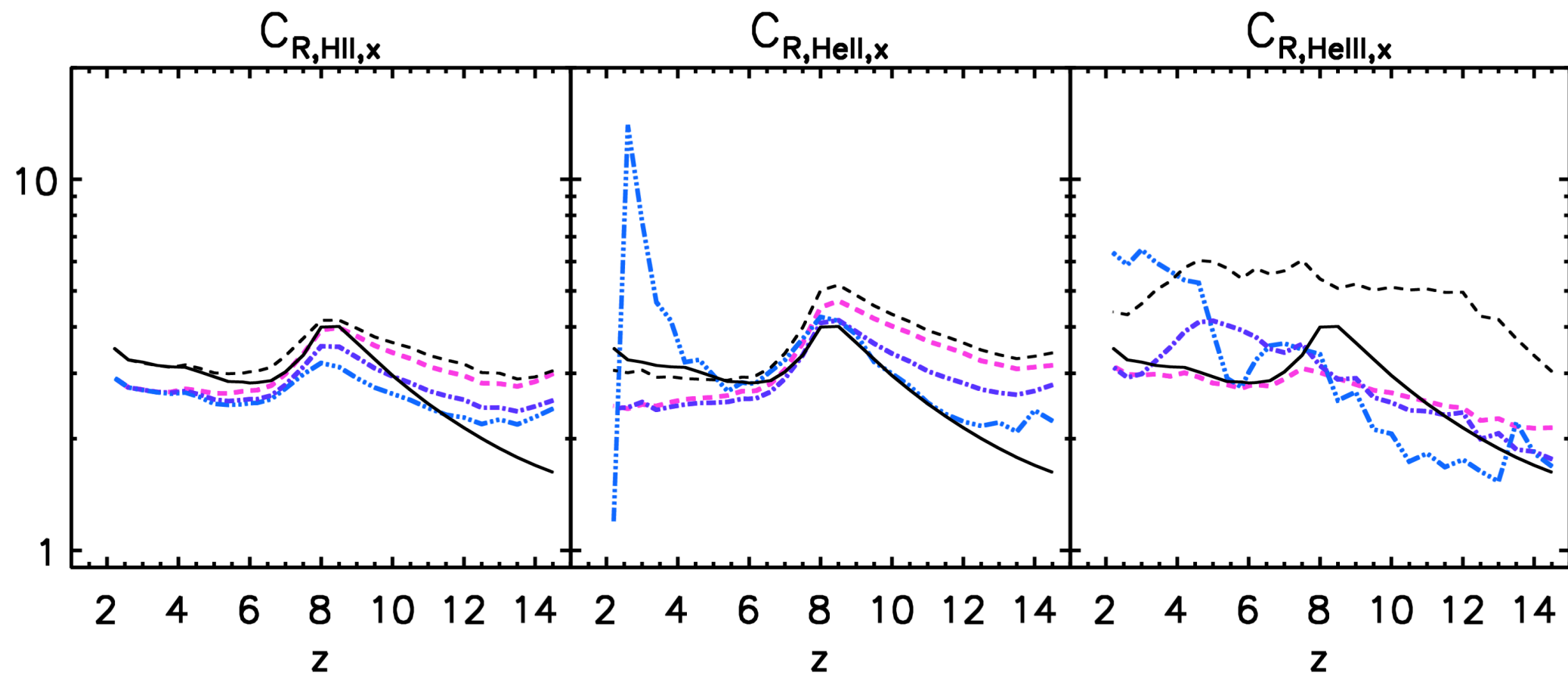
$x_{\text{HeIII}}=0.001$



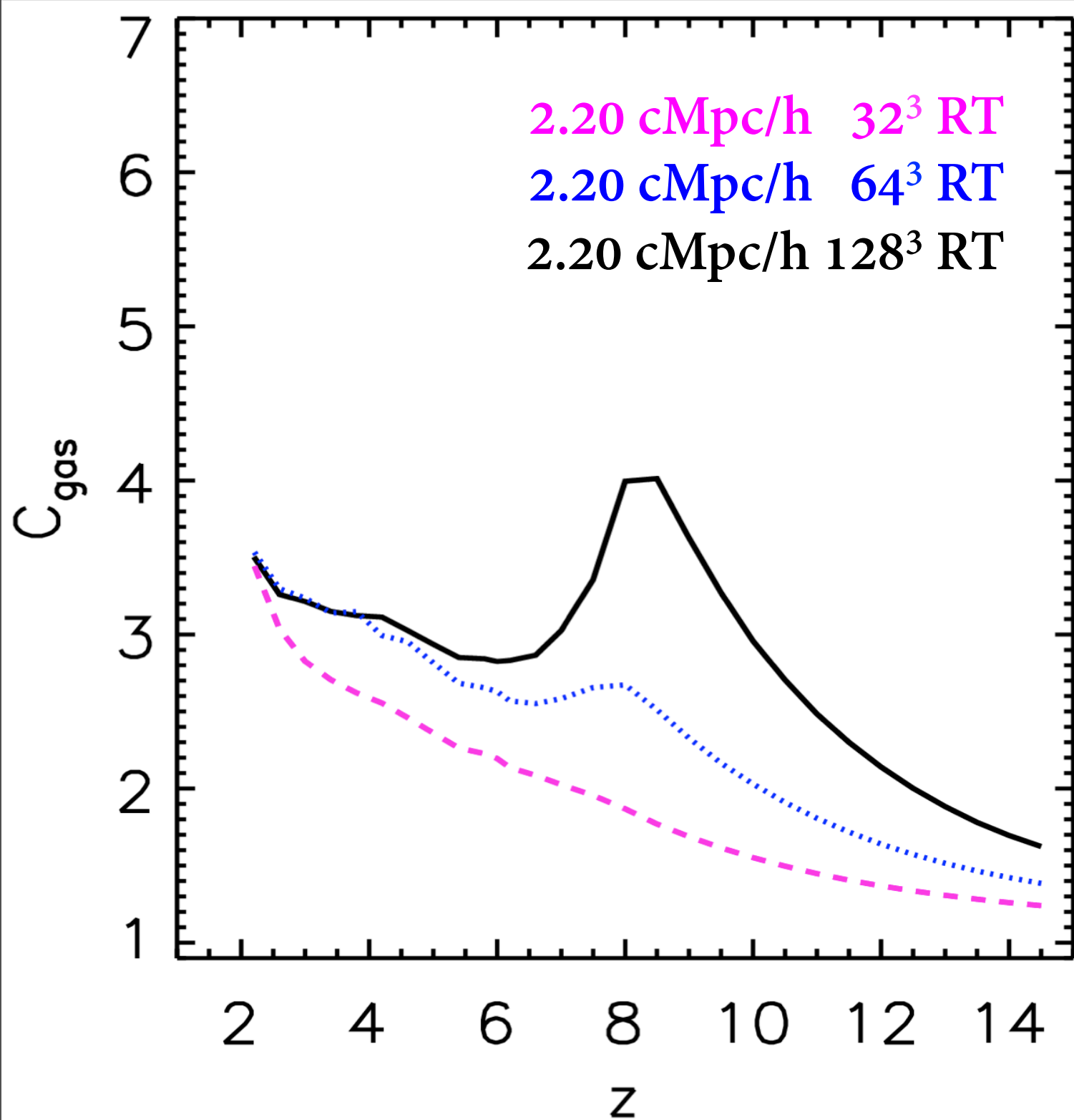
Effect of temperature dependent recombination rates

$$C_{R,i,x} = \langle n_i^* n_e^* \alpha_i(T) \rangle_{(x>x_{th})} / (\langle n_i \rangle_{(x>x_{th})}^* \langle n_e \rangle_{(x>x_{th})}^* \langle \alpha_i(T) \rangle_{(x>x_{th})})$$

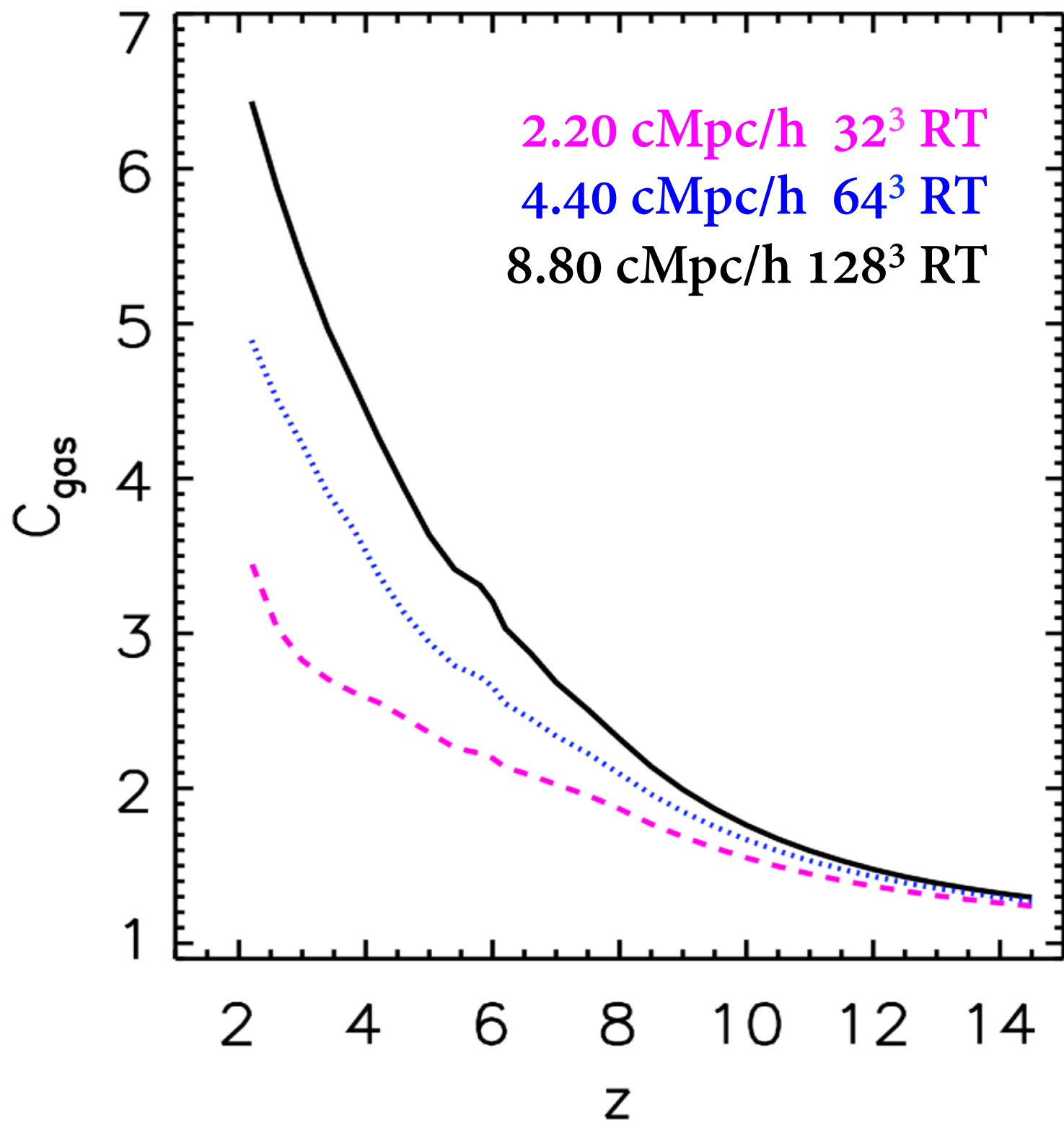
$\Delta_{\text{cell}} < 100$; Lines – C_{gas} , $x > 0$, $x > 0.1$, $x > 0.5$, $x > 0.9$



Grid size test



Box size test



Overdensity of the region

4.40 cMpc/h 128³ RT

divided to
8 equal sub-boxes
equivalent to

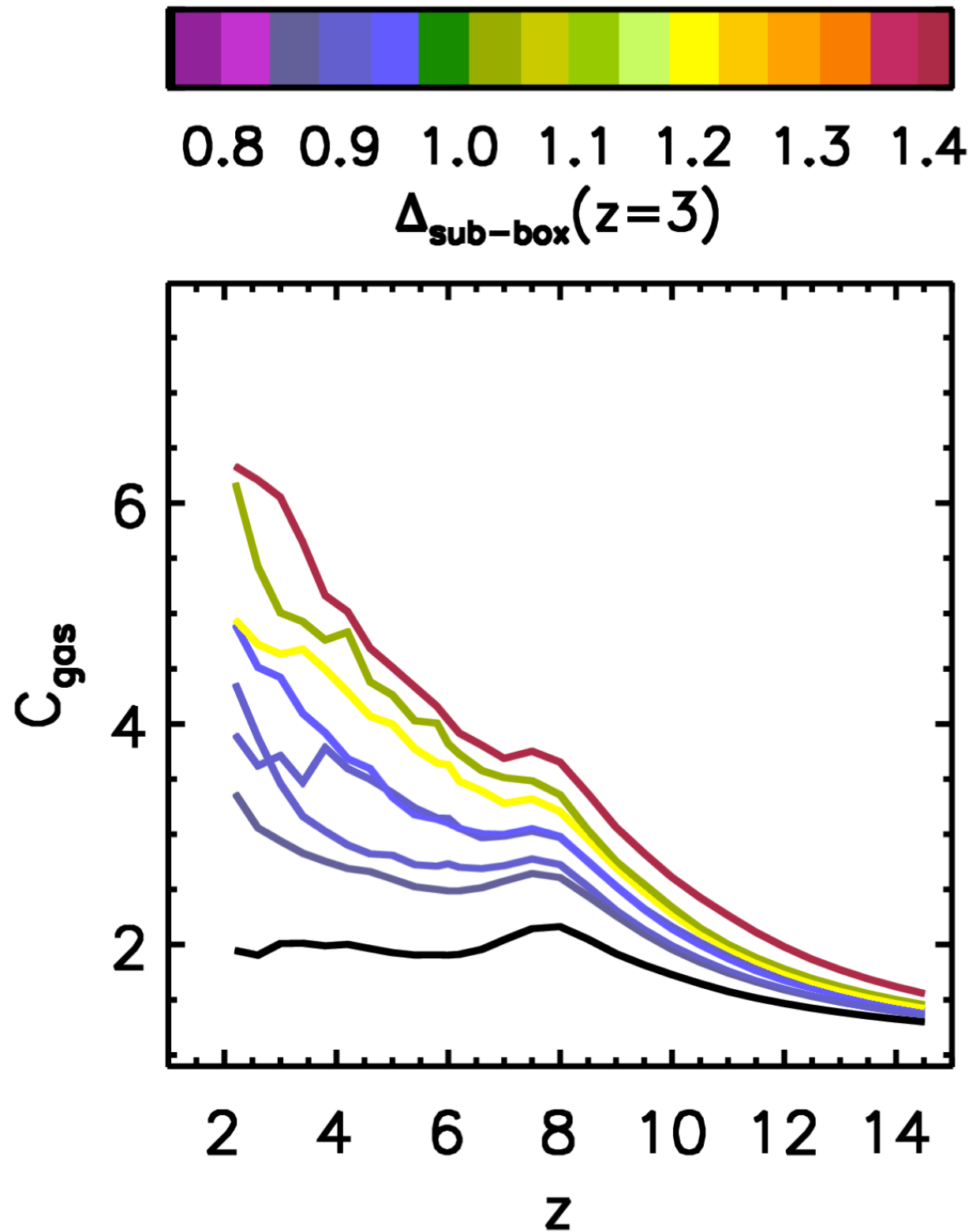
2.20 cMpc/h 64³ RT

$$\Delta_{\text{sub-box}} = \langle n_{\text{gas}} \rangle_{\text{sub-box}} / \langle n_{\text{gas}} \rangle_{\text{box}}$$

$$C_{\text{gas}} = \langle n_{\text{gas}}^2 \rangle / \langle n_{\text{gas}} \rangle^2$$

$$\Delta_{\text{cell}} < 100$$

Also seen by Kohler et al 2007,
Reicevic & Theuns 2011



Conclusions

- C_{gas} is consistent with previous values calculated for $z > 6$.
- $C_{\text{R},i,0.1}$ for $i=\text{HII}$, HeII and HeIII are close to C_{gas} .

But clumping factors do depend on box size and mean overdensity of the region. Therefore, the range needs to be explored.